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# Understanding of Long-Term Stability and Acceleration Factor

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Slide 1

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## Automotive Topics

- Long-Term Stability (Life-Time Shift)
  - for specs centered around a zero or a mean value
  - for parameters defined as an absolute value
- Thermal Acceleration Factor (AF)
  - Arrhenius equation and the Acceleration Factor
  - Effect of AF on the life of a product
  - Q100 Grade 1 vs 0 based on Thermal Profile

# Long-Term Stability

# Normal Gaussian Distribution

## Standard deviation and confidence intervals

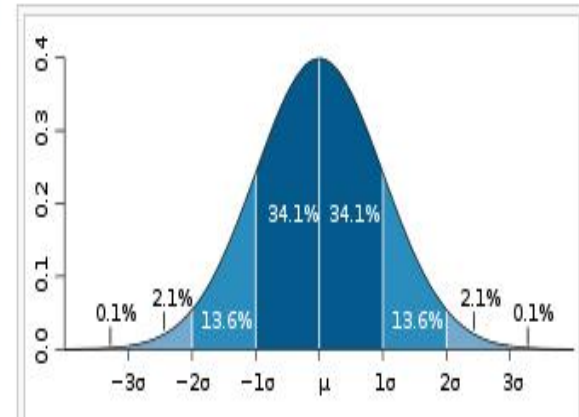
[edit]


About 68% of values drawn from a normal distribution are within one standard deviation  $\sigma$  away from the mean; about 95% of the values lie within two standard deviations; and about 99.7% are within three standard deviations. This fact is known as the *68-95-99.7 rule*, or the *empirical rule*, or the *3-sigma rule*. To be more precise, the area under the bell curve between  $\mu - n\sigma$  and  $\mu + n\sigma$  is given by

$$F(\mu + n\sigma; \mu, \sigma^2) - F(\mu - n\sigma; \mu, \sigma^2) = \Phi(n) - \Phi(-n) = \operatorname{erf}\left(\frac{n}{\sqrt{2}}\right),$$

where erf is the *error function*. To 12 decimal places, the values for the 1-, 2-, up to 6-sigma points are:<sup>[16]</sup>

| $n$ | $\operatorname{erf}\left(\frac{n}{\sqrt{2}}\right)$ | i.e. 1 minus ...  | or 1 in ...      |
|-----|---|-------------------|------------------|
| 1   | 0.682 689 492 137                                   | 0.317 310 507 863 | 3.151 487 187 53 |
| 2   | 0.954 499 736 104                                   | 0.045 500 263 896 | 21.977 894 5080  |
| 3   | 0.997 300 203 937                                   | 0.002 699 796 063 | 370.398 347 345  |
| 4   | 0.999 936 657 516                                   | 0.000 063 342 484 | 15,787.192 7673  |
| 5   | 0.999 999 426 697                                   | 0.000 000 573 303 | 1,744,277.893 62 |
| 6   | 0.999 999 998 027                                   | 0.000 000 001 973 | 506,797,345.897  |



Dark blue is less than one *standard deviation* from the *mean*.   
 For the normal distribution, this accounts for about 68% of the set, while two standard deviations from the mean (medium and dark blue) account for about 95%, and three standard deviations (light, medium, and dark blue) account for about 99.7%.

# Life-Time Shift Qual Guidelines

In a case of specs centered around zero or a mean value like Vos, Vos Drift, Vref, AOL, etc., they may shift over 10-year life up to:

**+/-100% of the max (min) PDS specified value**

In a case of parameters specified as an absolute value like IQ, Slew Rate (SR), Isc, etc. they may shift over 10-year life up to:

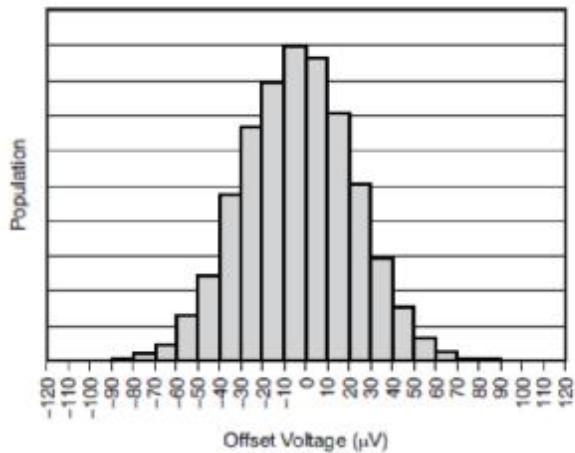
**+/-10% of the max (min) PDS specified value**

# Understanding Statistical Distributions

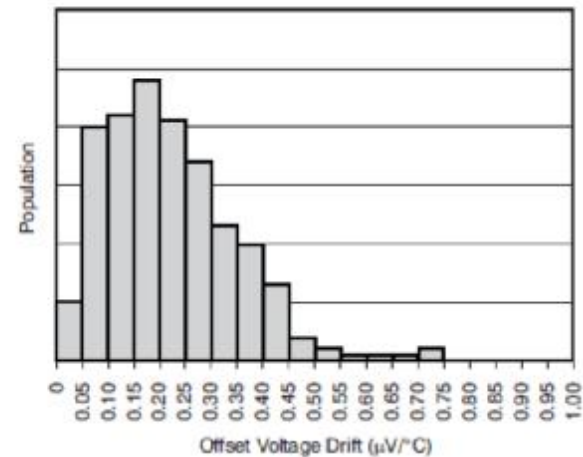
(specs centered around a zero)

| PARAMETER             | CONDITIONS      | OPA140, OPA2140, OPA4140 |            |     | UNIT             |
|-----------------------|-----------------|--------------------------|------------|-----|------------------|
|                       |                 | MIN                      | TYP        | MAX |                  |
| <b>OFFSET VOLTAGE</b> |                 |                          |            |     |                  |
| Offset Voltage, RTI   | $V_{OS}$        | $V_S = \pm 18V$          | 30         | 120 | $\mu V$          |
| Over Temperature      | $V_S = \pm 18V$ |                          |            | 220 | $\mu V$          |
| Drift                 | $dV_{OS}/dT$    | $V_S = \pm 18V$          | $\pm 0.35$ | 1.0 | $\mu V/^\circ C$ |

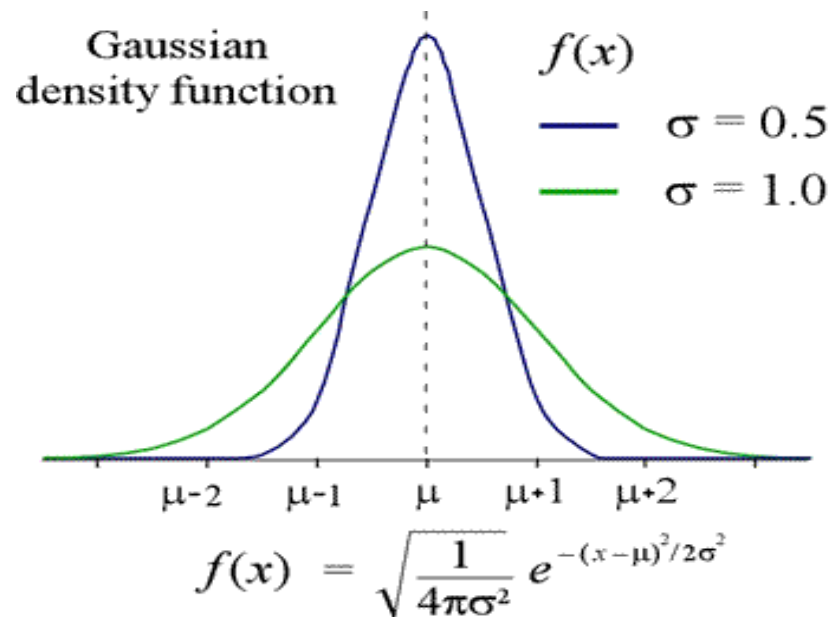
OFFSET VOLTAGE PRODUCTION DISTRIBUTION



OFFSET VOLTAGE DRIFT DISTRIBUTION



# Long-Term Shift for Normal Gaussian Distributions (Centered around a Mean Value)



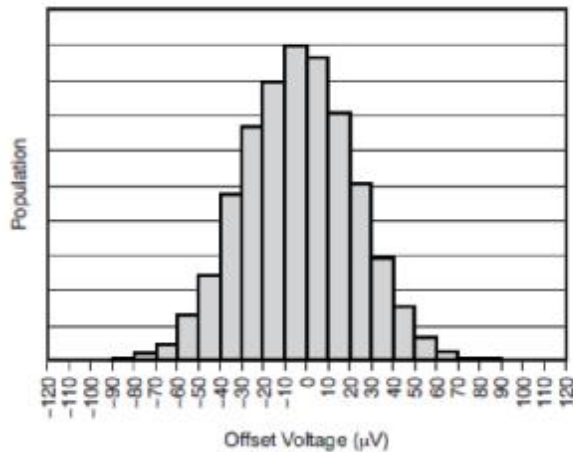
Initial PDS Distribution (blue) vs Long-Term Parametric Shift (green)



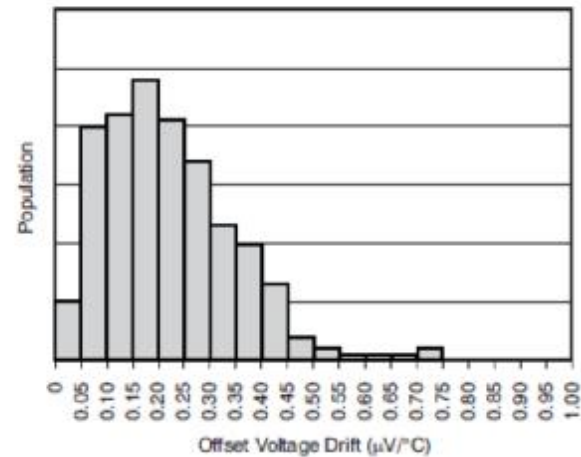
# Life-Time Vos and Vos Temp Drift Shift

| PARAMETER             | CONDITIONS   | OPA140, OPA2140, OPA4140 |            |     | UNIT                         |
|-----------------------|--------------|--------------------------|------------|-----|------------------------------|
|                       |              | MIN                      | TYP        | MAX |                              |
| <b>OFFSET VOLTAGE</b> |              |                          |            |     |                              |
| Offset Voltage, RTI   | $V_{OS}$     |                          | 30         | 120 | $\mu\text{V}$                |
| Over Temperature      |              |                          |            | 220 | $\mu\text{V}$                |
| Drift                 | $dV_{OS}/dT$ |                          | $\pm 0.35$ | 1.0 | $\mu\text{V}/^\circ\text{C}$ |

OFFSET VOLTAGE PRODUCTION DISTRIBUTION



OFFSET VOLTAGE DRIFT DISTRIBUTION



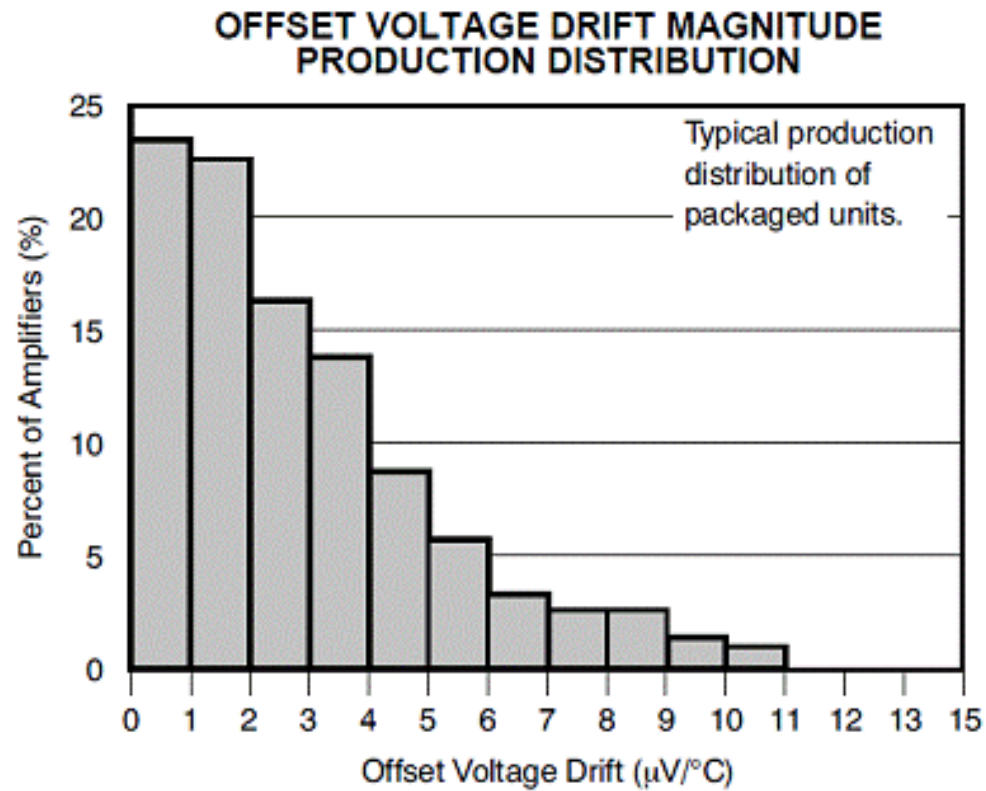
Max LT Vos = 240uV

Max LT Vos Drift = 2.0uV/C

Life-Time Max Shift (ten-year) = Max Initial Value

Long-Term Max Spec = 2 \* Initial Spec

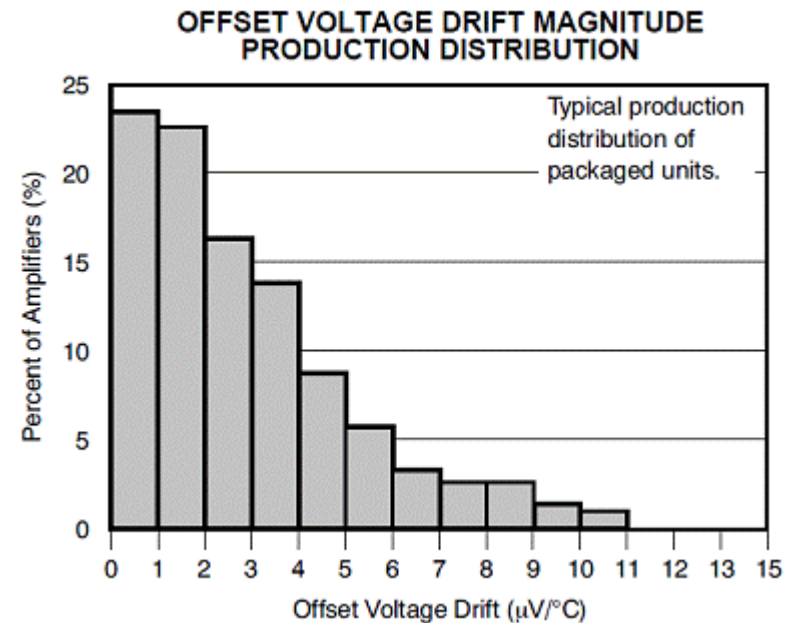
# What is the Vos Drift Maximum Value?



# Use of the Statistics to Determine Relative Maximum Value

Estimating a value of standard deviation (sigma)

| $n$ | $\text{erf}\left(\frac{n}{\sqrt{2}}\right)$ | i.e. 1 minus ...  | or 1 in ...      |
|-----|---|-------------------|------------------|
| 1   | 0.682 689 492 137                           | 0.317 310 507 863 | 3.151 487 187 53 |
| 2   | 0.954 499 736 104                           | 0.045 500 263 896 | 21.977 894 5080  |
| 3   | 0.997 300 203 937                           | 0.002 699 796 063 | 370.398 347 345  |
| 4   | 0.999 936 657 516                           | 0.000 063 342 484 | 15,787.192 7673  |
| 5   | 0.999 999 426 697                           | 0.000 000 573 303 | 1,744,277.893 62 |
| 6   | 0.999 999 998 027                           | 0.000 000 001 973 | 506,797,345.897  |



Knowing one-sigma is about ~4uV/C, customer may assume the maximum offset drift to be:

**12uV/C** (3\*sigma) where 1 out of 370 units will NOT meet this max spec

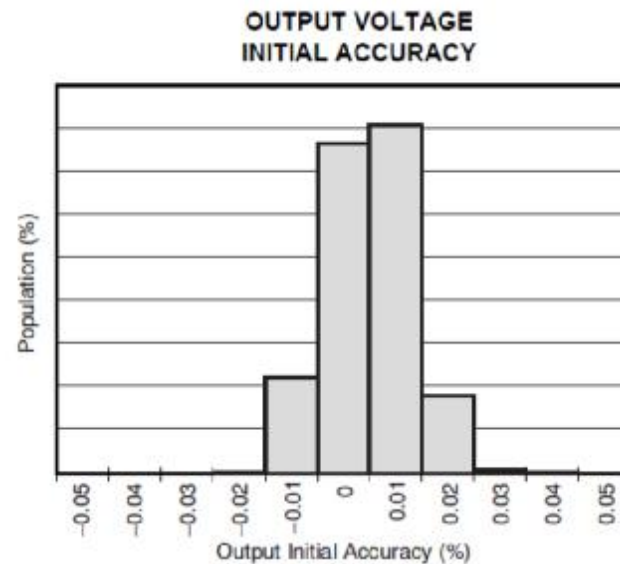
**16uV/C** (4\*sigma) where 1 out of 15,787 units will NOT meet this max spec

**20uV/C** (5\*sigma) where 1 out of 1,744,277 units will NOT meet this max spec

**24uV/C** (6\*sigma) where 1 out of 506,797,345 units will NOT meet this max spec

# Life-Time Reference Voltage Initial Accuracy Shift (specs centered around a mean value)

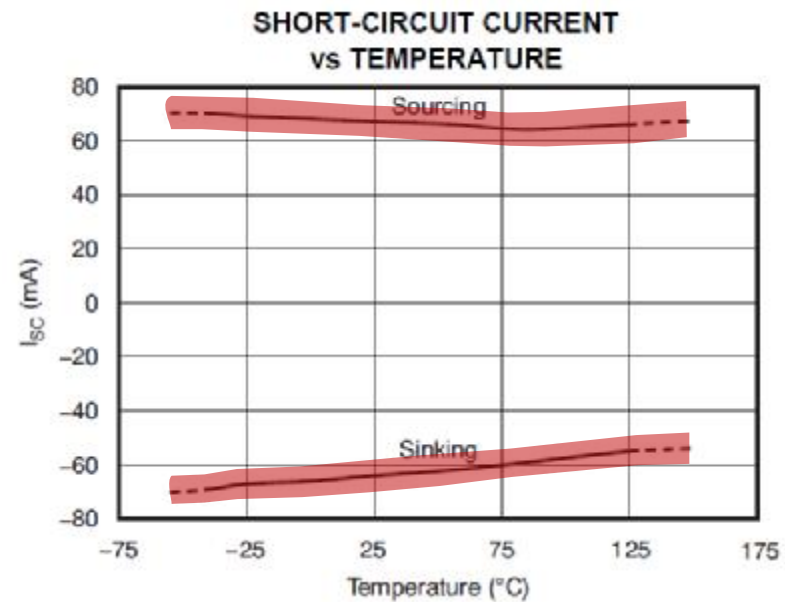
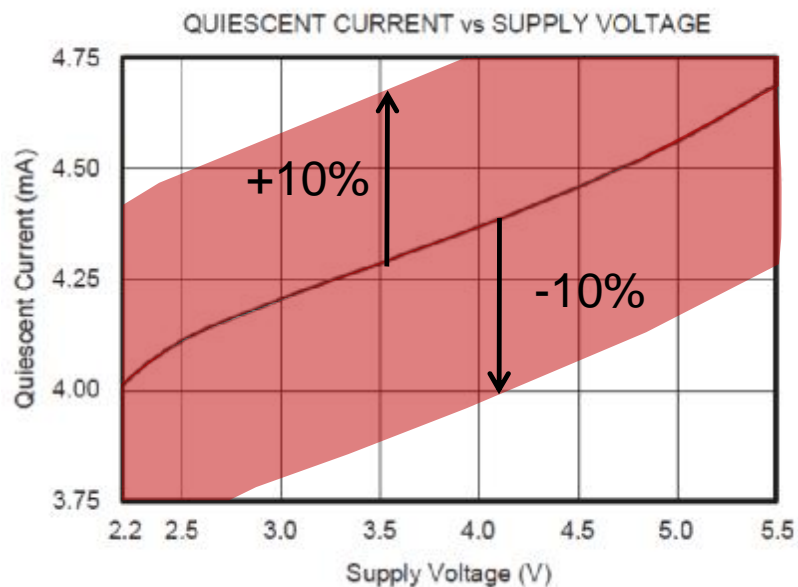
| PARAMETER                                     | CONDITIONS            | PER DEVICE |       |      | UNIT |
|---|-----------------------|------------|-------|------|------|
|   |                       | MIN        | TYP   | MAX  |      |
| REF5020 ( $V_{OUT} = 2.048V$ ) <sup>(1)</sup> |                       |            |       |      |      |
| OUTPUT VOLTAGE                                |                       |            |       |      |      |
| Output Voltage                                | $V_{OUT}$             |            | 2.048 |      | V    |
| Initial Accuracy: High-Grade                  | $2.7V < V_{IN} < 18V$ | -0.05      |       | 0.05 | %    |



Max LT Vref = +/-0.1%

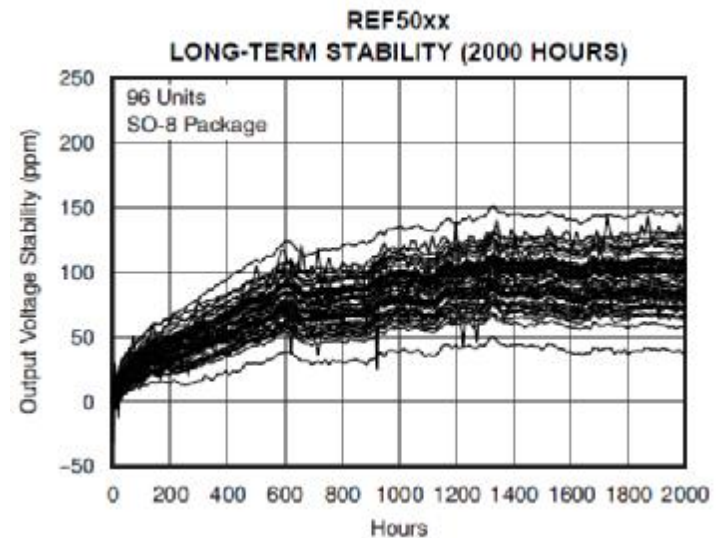
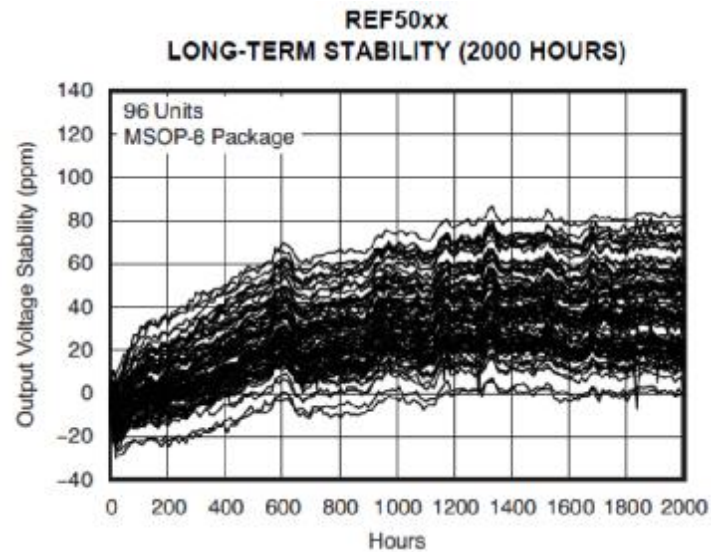
# Long-Term IQ and Isc Shift (specs centered around an absolute value)

| PARAMETER                            |          | CONDITIONS     | OPA827AI |          |     | UNIT |
|--------------------------------------|----------|----------------|----------|----------|-----|------|
|                                      |          |                | MIN      | TYP      | MAX |      |
| Quiescent Current<br>(per amplifier) | $I_Q$    | $I_{OUT} = 0A$ |          | 4.8      | 5.2 | mA   |
| Short-Circuit Current                | $I_{SC}$ |                | $\pm 55$ | $\pm 65$ |     | mA   |



# Long-Term Vref Stability

| PARAMETER                  | CONDITIONS         | REF50xx |     |     | UNIT        |
|----------------------------|--------------------|---------|-----|-----|-------------|
|                            |                    | MIN     | TYP | MAX |             |
| <b>LONG-TERM STABILITY</b> |                    |         |     |     |             |
| MSOP-8                     | 0 to 1000 hours    |         | 50  |     | ppm/1000 hr |
| MSOP-8                     | 1000 to 2000 hours |         | 5   |     | ppm/1000 hr |
| SO-8                       | 0 to 1000 hours    |         | 90  |     | ppm/1000 hr |
| SO-8                       | 1000 to 2000 hours |         | 10  |     | ppm/1000 hr |



# Life-Time Shift Formula

To illustrate the life-time shift for an actual IC, let's consider the long-term stability of the low-noise, low-drift [REF5025 precision voltage reference](#) and its output initial accuracy specification.

Figure 3 shows the initial accuracy of [REF5025](#) output voltage of  $\pm 0.05\%$  and the long-term stability for 0 to 1000 hours specified at 50ppm. As explained above, the long-term shift of the [REF5025](#) must not exceed the life-test shift of  $\pm 100\%$  of the max/min initial accuracy; therefore, the maximum output voltage shift after 10 years (87,600 hours), under constant operation at room temperature, must be less than  $\pm 0.05\%$ , or an equivalent of  $\pm 500$ ppm.

| PARAMETER           | CONDITIONS         | REF50xx |     |     | UNIT        |
|---------------------|--------------------|---------|-----|-----|-------------|
|                     |                    | MIN     | TYP | MAX |             |
| LONG-TERM STABILITY |                    |         |     |     |             |
| MSOP-8              | 0 to 1000 hours    |         | 50  |     | ppm/1000 hr |
| MSOP-8              | 1000 to 2000 hours |         | 5   |     | ppm/1000 hr |

| PARAMETER                    | CONDITIONS                                   | PER DEVICE |       |      | UNIT |
|------------------------------|--|------------|-------|------|------|
|                              |  | MIN        | TYP   | MAX  |      |
|                              | REF5020 ( $V_{out} = 2.048V$ ) <sup>1)</sup> |            |       |      |      |
| OUTPUT VOLTAGE               |  |            |       |      |      |
| Output Voltage               | $V_{out}$                                    |            | 2.048 |      | V    |
| Initial Accuracy: High-Grade | $2.7V < V_{in} < 18V$                        | -0.05      |       | 0.05 | %    |

Figure 3 - Excerpts from [REF5025](#) datasheet

Since the long-term shift clearly cannot be a linear function of time and simultaneously satisfy both conditions, the shift rate must initially be higher (having a steeper slope) and then gradually slow down (becoming more linear) over time. Therefore, it may be estimated by the square-root function normalized to 1000<sup>th</sup> of hours and shown below in Figure 4.

$$\text{Output Voltage Shift} = 50\text{ppm} \cdot \sqrt{[\text{time}(\text{hours})/1000\text{hrs}]}$$

# Life-Time Shift Estimation Graph

$$\text{Output Voltage Shift} = 50\text{ppm} \cdot \sqrt{[\text{time}(\text{hours})/1000\text{hrs}]}$$



Figure 4 – REF5025 long-term stability

For example, after 25,000 hours of nonstop operation in the field, the typical output voltage shift in the REF5025 can be calculated using above equation,  $50\text{ppm} \cdot \sqrt{25} = 250\text{ppm}$ , while after 10 years (87,600 hours) the shift would be  $50\text{ppm} \cdot \sqrt{87.6} = 468\text{pp}$ . Therefore, at the end-of-life the REF5025 output voltage shift as expected is within the 500ppm allowable shift which equals to 0.05% of the datasheet maximum initial accuracy spec.



# Life-Time Shift Rule Summary

You may estimate the maximum expected parametric shift over any given period of time by using:

- **100% of the max (min) PDS guaranteed value in the case of specs centered around a mean value** (Vos, Vos Drift, Vref, AOL, etc.)
- **10% of the max (min) guaranteed value for parameters specified as an absolute value** (IQ, slew rate, Isc, etc).

One may pro-rate the shift based on the expected ten-year life of the product

It needs to be understood that the long-term shift is NOT exactly a linear function of time – the shift is greater (curve is steeper) initially and slows down (become linear) over time. Therefore, the linear character of shift usually excludes the first month due to continuing self-curing of the molding compound used for packaging of IC.

# Acceleration Factor

# HTOL (High Temperature Operating Life)

- HTOL is used to measure the constant failure rate region at the bottom of the bathtub curve as well as to assess the wear-out phase of the curve for some use conditions.
- Smaller sample sizes than EFR but are run for a much longer duration
- Jedec and QSS default are  $T_a=125C$  for 1000 hours
- Q100 calls for 1000 hours at max temperature for the device's grade
- Most modern IC's undergo HTOL at  $T_a=150C$  for 300 hours

# The Arrhenius Equation

The Arrhenius equation is a simple, but remarkably accurate, formula for the temperature dependence of the reaction rate constant of a process.

$$\text{Process Rate (PR)} = Ae^{-(Ea/kT)}$$

**A = A constant**

**Ea = Thermal activation energy in electron-volts (eV)**

**k = Boltzman's constant,  $8.62 \times 10^{-5}$  eV/K**

**T = Absolute temperature in degrees Kelvin (Deg C + 273.15)**

# Acceleration Factor

Acceleration Factors are the ratio of the Process Rate at two temperatures.

$$AF(T1 \text{ to } T2) = PR2 / PR1 = Ae^{-(Ea/kT2)} / Ae^{-(Ea/kT1)}$$

$$AF(T1 \text{ to } T2) = e^{(Ea/k)(1/T1 - 1/T2)}$$

A = A constant (has canceled out of the formula)

Ea = Thermal activation energy in electron volts (eV)

k = Boltzman's constant,  $8.62 \times 10^{-5}$  eV/K

T = Absolute temperature in degrees Kelvin (degrees C + 273.15)

# Acceleration Factors Calculation Example

Calculate the thermal acceleration factor (AF) between the stress test temperature at 150C and the product junction temperature of **53C**:

T1 (application) = 53C -> 326K

T2 (life-test stress) =150C -> 423K

Ea=0.7eV

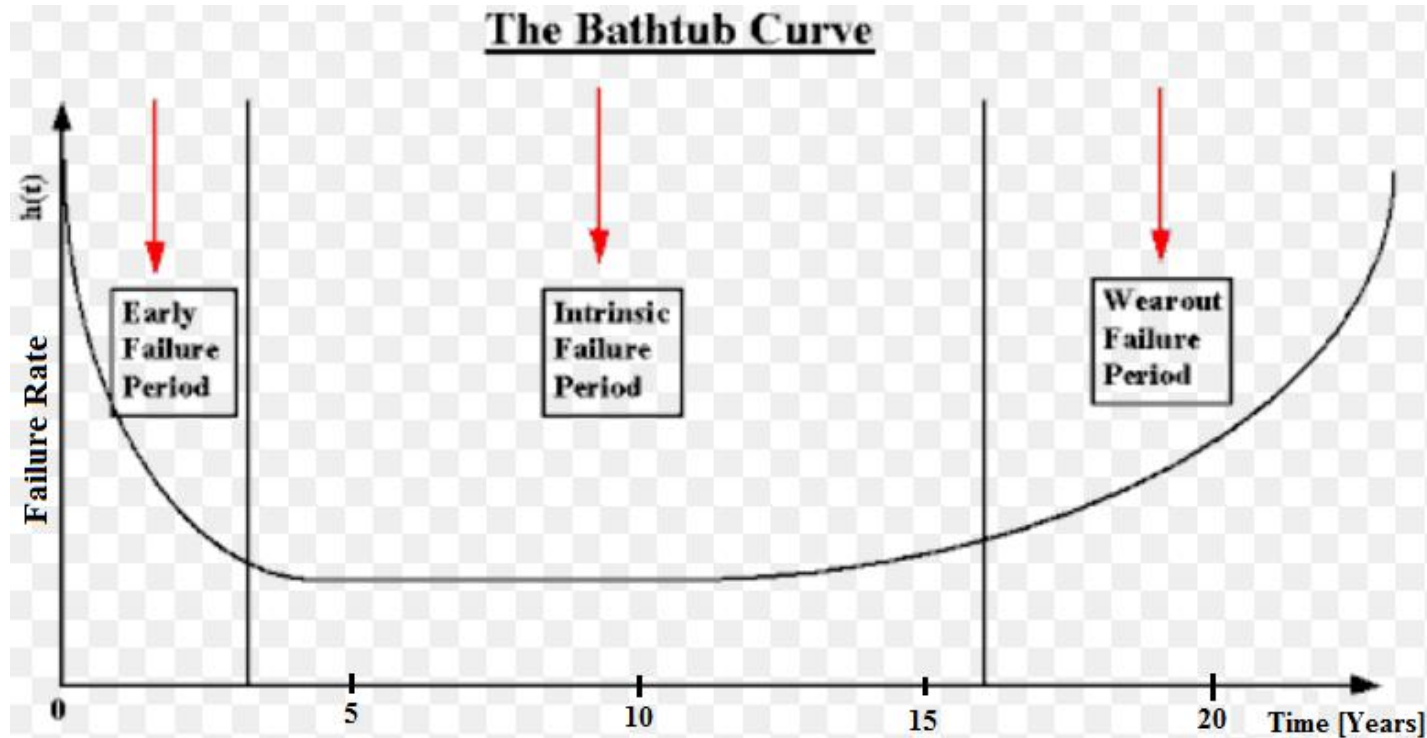
$$\mathbf{AF(53C\ to\ 150C)} = e^{(0.7\text{eV}/8.62 \times 10^{-5})(1/326 - 1/423)} = \mathbf{303}$$

This means every hour of stress at 150C is equivalent to 303 hours of use in the application at 53 deg C junction temperature.

Thus 300-hour life-test at 150C used to qualify the product would cause similar shift as 90,762 hours (303\*300hrs), or about 10 years, in the field at 53C junction (25C ambient temperature).

# Semiconductor Quality and Reliability

| Part number | Early life failure rate | MTBF / FIT         |     | Early life failure rate supporting data |                |             |       | MTBF / FIT supporting data |                |                        |                |                       |             |       |
|-------------|-------------------------|--------------------|-----|---|----------------|-------------|-------|----------------------------|----------------|------------------------|----------------|-----------------------|-------------|-------|
|             | ELFR-DPPM               | MTBF               | FIT | Conf level (%)                          | Test temp (°C) | Sample size | Fails | Usage temp (°C)            | Conf level (%) | Activation energy (eV) | Test temp (°C) | Test duration (hours) | Sample size | Fails |
| OPA192ID    | 22                      | $4.89 \times 10^9$ | 0.2 | 60                                      | 125            | 41306       | 0     | 55                         | 60.0           | 0.7                    | 125            | 1000                  | 57098       | 0     |



# Questions ?

***Comments, Questions, Technical Discussions Welcome:***

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