## Bi-quad filters realization on AIC Codecs

HPA SoftwareABSTRACTThis application report provides information regarding filter equations and co-efficient format representation thatcan be used to realize digital filters on the AIC3xxx miniDSP platform. It also explains ways to update the filtercoefficients on the fly using a host processor.
Contents
1 Standard Bi-quad filter equations ..... 2
1.1 All Pass (Phase shift) filters ..... 2
1.2 Equalization filters ..... 3
1.3 Notch Filters ..... 5
1.4 Treble Shelf ..... 7
1.5 Bass Shelf Filters ..... 9
1.6 Second order Linkwitz Riley ..... 12
1.7 Second Order Variable Q Filter ..... 13
1.8 Second order Butterworth Filter from Variable Q. ..... 15
1.9 Second order Bessel Filter from Variable Q ..... 15
1.10 First Order Butterworth Filters ..... 15
1.11 Second order Chebychev ..... 17
2 Number representation format for filter coefficients ..... 21
2.1 Filter coefficient normalization. ..... 22
3 Updating the codec filter coefficients ..... 23
Appendix A. Biquad coefficients computation example ..... 25
Figures
Figure 1. Phase shift filter phase response ( $\mathrm{F}_{\mathrm{c}}=1200 \mathrm{~Hz}, \mathrm{BW}=\mathbf{3 0 0 H z}$ ) ..... 2
Figure 2. EQ filter with $F_{c}=1 \mathrm{kHz}, B W=100 \mathrm{~Hz}, G=6 \mathrm{~dB}$ ..... 4
Figure 3. Notch filter magnitude response with $F_{c}=1 \mathrm{kHz}, \mathrm{BW}=100 \mathrm{~Hz}$ ..... 6
Figure 4. Treble shelf filter magnitude response ( $F_{c}=2 \mathrm{kHz}, \mathrm{G}=-6 \mathrm{~dB}$ ) ..... 8
Figure 5. Bass shelf filter magnitude response $\left(F_{c}=500 \mathrm{~Hz}, G=6 \mathrm{~dB}\right)$ ..... 10
Figure 6. Second order Linkwitz Riley ( $\mathrm{F}_{\mathrm{c}}=500 \mathrm{~Hz}$, HL=high) ..... 12
Figure 7. Second order variable $Q$ filter $\left(F_{c}=1200 \mathrm{~Hz}, \mathrm{Q}=1, \mathrm{HL}=\mathrm{low}\right)$ ..... 14
Figure 8. First order Butterworth $\left(\mathrm{F}_{\mathrm{c}}=1200 \mathrm{~Hz}, \mathrm{HL}=\mathrm{low}\right)$ ..... 16
Figure 9. Second order Chebychev ( $\mathrm{F}_{\mathrm{c}}=600 \mathrm{~Hz}$, typ=high, rip=3dB) ..... 19
Figure 10. Normalizing filter response ..... 23
Tables
Table 1. EQ Filter coefficients table in host controller for "enhanced" codecs ..... 24

## 1 Standard Bi-quad filter equations

### 1.1 All Pass (Phase shift) filters

Filter parameters
BW = Bandwidth in Hz
$\mathrm{F}_{\mathrm{c}}=$ Center frequency in Hz
$\mathrm{F}_{\mathrm{s}}=$ Sample frequency in Hz

## Error Checking

$0 \leq B W \leq \frac{F_{s}}{2}$
$0 \leq F_{c} \leq \frac{F_{s}}{2}$
$0 \leq F_{s} \leq 192 K$


Figure 1. Phase shift filter phase response ( $F_{c}=1200 \mathrm{~Hz}, \mathrm{BW}=300 \mathrm{~Hz}$ )

## Equation

$$
\begin{aligned}
& a= \frac{1-\tan \left(\pi \times \frac{B W}{F_{s}}\right)}{1+\tan \left(\pi \times \frac{B W}{F_{s}}\right)} \\
& d=-\cos \left(2 \times \pi \times \frac{F_{c}}{F_{s}}\right)
\end{aligned}
$$

## Filter Coefficients

$$
\begin{aligned}
& b 0=a \\
& b 1=d \times(1+a) \\
& a 1=b 1 \\
& b 2=1 \\
& a 2=a \\
& B=\left[\begin{array}{lll}
b 0 & b 1 & b 2
\end{array}\right] \\
& A=\left[\begin{array}{lll}
1 & a & a
\end{array}\right]
\end{aligned}
$$

### 1.2 Equalization filters

## Filter Parameters

BW = Filter Bandwidth in Hz
$\mathrm{F}_{\mathrm{c}}=$ Filter Center Frequency in Hz
$\mathrm{F}_{\mathrm{s}}=$ Sample rate in Hz
$\mathrm{G}=$ Filter Gain in dB

## Error Checking

$0 \leq B W \leq \frac{F_{s}}{2}$
$0 \leq F_{c} \leq \frac{F_{s}}{2}$
$0 \leq F_{s} \leq 192 K$
$-140 \leq G \leq 48$


Figure 2. $E Q$ filter with $F_{c}=1 \mathrm{kHz}, \mathrm{BW}=100 \mathrm{~Hz}, \mathrm{G}=6 \mathrm{~dB}$

Equation

$$
\begin{aligned}
& \begin{array}{l}
A=10^{\frac{G}{20}} \\
\text { if }(A<1) \\
a
\end{array} \\
& \text { else } \\
& \qquad a=\frac{\left(\tan \left(\pi \times \frac{B W}{F_{s}}\right)-A\right)}{\left(\tan \left(\pi \times \frac{B W}{F_{s}}\right)+A\right)} \\
& H=A-1 \\
& \left.d=-\tan \left(\pi \times \frac{B W}{F_{s}}\right)-1\right) \\
& \left.t\left(2 \times \pi \times \frac{B W}{F_{s}}\right)+1\right) \\
& F_{s}
\end{aligned}
$$

## Filter Coefficients

$b 0=1+(1+a) \times \frac{H}{2}$
$b 1=d \times(1+a)$
$b 2=\left(-a-(1+a) \times \frac{H}{2}\right)$
$a 1=b 1$
$a 2=-a$
$B=\left[\begin{array}{lll}b 0 & b 1 & b 2\end{array}\right]$
$A=\left[\begin{array}{lll}1 & a & a\end{array}\right]$

### 1.3 Notch Filters

## Filter Parameters

BW = Notch Bandwidth in Hz
$\mathrm{F}_{\mathrm{c}}=$ Notch Center frequency in Hz
$\mathrm{F}_{\mathrm{s}}=$ Sample rate in Hz

## Error Checking

$0 \leq B W \leq \frac{F_{s}}{2}$
$0 \leq F_{c} \leq \frac{F_{s}}{2}$
$0 \leq F_{s} \leq 192 K$


Figure 3. Notch filter magnitude response with $\mathrm{F}_{\mathrm{c}}=1 \mathrm{kHz}, \mathrm{BW}=\mathbf{1 0 0 H z}$

## Equation

$$
\begin{aligned}
a & =\frac{1-\tan \left(\pi \times \frac{B W}{F_{s}}\right)}{1+\tan \left(\pi \times \frac{B W}{F_{s}}\right)} \\
d & =-\cos \left(2 \times \pi \times \frac{F_{c}}{F_{s}}\right) \\
b 0 & =a \\
b 1 & =d \times(1+a) \\
a 1 & =b 1 \\
b 2 & =1 \\
a 2 & =a
\end{aligned}
$$

## Filter Coefficients

$B=\left[\begin{array}{lll}b 0 & b 1 & b 2\end{array}\right]$
$A=\left[\begin{array}{lll}1 & a & a\end{array}\right]$
$B=0.5 \times(B+A)$

### 1.4 Treble Shelf

## Filter Parameters

$\mathrm{F}_{\mathrm{c}}=$ Treble Shelf Corner frequency in Hz
$\mathrm{F}_{\mathrm{s}}=$ Sample rate in Hz
$\mathrm{G}=$ Treble Shelf Gain in dB

## Error Checking

$0 \leq F_{c} \leq \frac{F_{s}}{2}$
$0 \leq F_{s} \leq 192 K$
$-24 \leq G \leq 24$


Figure 4. Treble shelf filter magnitude response $\left(F_{c}=2 k H z, G=-6 d B\right)$

## Equation

$g=10^{\frac{G}{20}}$
$s=\frac{\operatorname{sqrt}(2)}{2}$
$\rho=\frac{\pi}{2}$
$\varphi=\frac{F_{c}}{F_{s}} \times \pi$
$A=g$
$G=20 \times \log 10(A)$

INSTRUMENTS

$$
\begin{aligned}
& \text { If } \mathrm{G}>-6 \& \mathrm{G}<\mathrm{6} \\
& \mathrm{~F}=\operatorname{sqrt}(A) \\
& \text { elseif } \mathrm{A}>1
\end{aligned} \quad \begin{aligned}
& F=\frac{A}{\operatorname{sqrt}(2)} \\
& \text { else } \\
& \text { end } \quad F=A \times \operatorname{sqrt}(2) \\
& g d=\sqrt[4]{\frac{\left(F^{2}-1\right)}{A^{2}-F^{2}}} \\
& g n=s q r t(A) \times g d \\
& a=\tan \left(\pi \times\left(\frac{F_{c}}{F_{s}}-\frac{1}{4}\right)\right) \\
& b 0=\frac{g n^{2} \times a^{2}+2 \times s \times g n-2 \times g n^{2} \times a+1-2 \times s \times g n \times a^{2}+a^{2}+g n^{2}+2 \times a}{1+g d^{2}+2 \times s \times g d-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}-2 \times g d^{2} \times a+a^{2}+2 \times a} \\
& b 1=\frac{2-2 \times g n^{2} \times a^{2}+4 \times g n^{2} \times a+4 \times a-2 \times g n^{2}+2 \times a^{2}}{1+g d^{2}+2 \times s \times g d-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}-2 \times g d^{2} \times a+a^{2}+2 \times a} \\
& b 2=\frac{1+2 \times s \times g n \times a^{2}-2 \times s \times g n+2 \times a+a^{2}+g n^{2}-2 \times g n^{2} \times a+g n^{2} \times a^{2}}{1+g d^{2}+2 \times s \times g d-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}-2 \times g d^{2} \times a+a^{2}+2 \times a} \\
& a 0=1 \\
& a 1=\frac{1}{1+g d^{2}+2 \times s \times g d-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}-2 \times g d^{2} \times a+a^{2}+2 \times a} \\
& a 2=\frac{1-2 \times g d^{2} \times a+2 \times a+g d^{2}-2 \times s \times g d+a^{2}+g d^{2} \times a^{2}+2 \times s \times g d \times a^{2}}{1+g d^{2}+2 \times s \times g d-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}-2 \times g d^{2} \times a+a^{2}+2 \times a}
\end{aligned}
$$

## Filter Coefficients

$$
\left.\begin{array}{rl}
B & =\left[\begin{array}{lll}
b 0 & b 1 & b
\end{array}\right] \\
A & =\left[\begin{array}{lll}
a 0 & a & a
\end{array}\right]
\end{array}\right]
$$

### 1.5 Bass Shelf Filters

## Filter Parameters

$\mathrm{F}_{\mathrm{c}}=$ Bass Shelf Corner frequency in Hz
$\mathrm{F}_{\mathrm{s}}=$ Sample rate in Hz
$\mathrm{G}=$ Bass Shelf Gain in dB

## Error Checking

$$
\begin{aligned}
& 0 \leq F_{c} \leq \frac{F_{s}}{2} \\
& 0 \leq F_{s} \leq 192 K \\
& -24 \leq G \leq 24
\end{aligned}
$$



Figure 5. Bass shelf filter magnitude response $\left(F_{c}=500 \mathrm{~Hz}, \mathrm{G}=6 \mathrm{~dB}\right)$

## Equation

$$
\begin{aligned}
& g=10^{\frac{G}{20}} \\
& s=\frac{s q r t(2)}{2} \\
& \rho=\frac{\pi}{2} \\
& \varphi=\frac{F_{c}}{F_{s}} \times \pi \\
& A=g \\
& G=20 \times \log 10(A)
\end{aligned}
$$

$$
\begin{aligned}
& \text { If } G>-6 \& G<6 \\
& F=\operatorname{sqrt}(A) \\
& \text { elseif A > } 1 \\
& F=\frac{A}{\operatorname{sqrt}(2)} \\
& \text { else } \\
& F=A \times \operatorname{sqrt}(2) \\
& \text { end } \\
& g d=\sqrt[4]{\frac{\left(F^{2}-1\right)}{A^{2}-F^{2}}} \\
& g n=\operatorname{sqrt}(A) \times g d \\
& a=\tan \left(\pi \times\left(\frac{F_{c}}{F_{s}}-\frac{1}{4}\right)\right) \\
& b 0=\frac{-\left(-1-g n^{2} \times a^{2}-a^{2}-2 \times g n^{2} \times a-g n^{2}-2 \times s \times g n+2 \times s \times g n \times a^{2}+2 \times a\right)}{2 \times s \times g d+1-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}+2 \times g d^{2} \times a+a^{2}+g d^{2}-2 \times a} \\
& b 1=\frac{-\left(2-4 \times a-4 \times g n^{2} \times a-2 \times g n^{2} \times a^{2}-2 \times g n^{2}+2 \times a^{2}\right)}{2 \times s \times g d+1-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}+2 \times g d^{2} \times a+a^{2}+g d^{2}-2 \times a} \\
& b 2=\frac{1+2 \times s \times g n \times a^{2}-2 \times a+g n^{2}-2 \times s \times g n+2 \times g n^{2} \times a+a^{2}+g n^{2} \times a^{2}}{2 \times s \times g d+1-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}+2 \times g d^{2} \times a+a^{2}+g d^{2}-2 \times a} \\
& a 0=1 \\
& a 1=\frac{-2+2 \times g d^{2} \times a^{2}+4 \times g d^{2} \times a-2 \times a^{2}+2 \times g d^{2}+4 \times a}{2 \times s \times g d+1-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}+2 \times g d^{2} \times a+a^{2}+g d^{2}-2 \times a} \\
& a 2=\frac{g d^{2} \times a^{2}-2 \times a+1+2 \times g d^{2} \times a-2 \times s \times g d+a^{2}+2 \times s \times g d \times a^{2}+g d^{2}}{2 \times s \times g d+1-2 \times s \times g d \times a^{2}+g d^{2} \times a^{2}-2 \times g d^{2} \times a+a^{2}+g d^{2}-2 \times a}
\end{aligned}
$$

## Filter Coefficients

$B=\left[\begin{array}{lll}b 0 & b 1 & b 2\end{array}\right]$
$A=\left[\begin{array}{lll}a & a & a\end{array} a 2\right]$

### 1.6 Second order Linkwitz Riley

Filter Parameters
$\mathrm{F}_{\mathrm{s}}=$ Sample rate in Hz
$\mathrm{F}_{\mathrm{c}}=$ Cut frequency in Hz
HL=LR Filter type (high, low)
Error Checking
$0 \leq F_{c} \leq \frac{F_{s}}{2}$
$0 \leq F_{s} \leq 192 K$
$H L=(h i g h, l o w)$


Figure 6. Second order Linkwitz Riley ( $\mathrm{F}_{\mathrm{c}}=500 \mathrm{~Hz}$, HL=high)

## Equation

$$
\begin{aligned}
& \left.\begin{array}{l}
w c=2 \times \pi \times F_{c} \\
\text { if } H L(1: 3)=='^{\prime} l o w^{\prime} \\
B a
\end{array}\right]\left[\begin{array}{lll}
0 & 0 & w c^{2}
\end{array}\right] \\
& A a=\left[\begin{array}{lll}
1 & 2 \times w c & w c^{2}
\end{array}\right] \\
& \text { else } \\
& \qquad B a=\left[\begin{array}{lll}
1 & 0 & 0
\end{array}\right] \\
& \quad A a=\left[\begin{array}{lll}
1 & 2 \times w c & w c^{2}
\end{array}\right] \\
& \text { end } \\
& k=2 \times \pi \times \frac{F_{c}}{\tan \left(\pi \times \frac{F_{c}}{F_{s}}\right)} \\
& B=\left[B a(1) \times k^{2}+B a(3)+B a(2) \times k,-2 \times B a(1) \times k^{2}+2 \times B a(3),-B a(2) \times k+B a(1) \times k^{2}+B a(3)\right] \\
& A=\left[A a(1) \times k^{2}+A a(3)+A a(2) \times k,-2 \times A a(1) \times k^{2}+2 \times A a(3),-A a(2) \times k+A a(1) \times k^{2}+A a(3)\right]
\end{aligned}
$$

## Filter Coefficients

$B=\frac{B}{A(1)}$
$A=\frac{A}{A(1)}$

### 1.7 Second Order Variable Q Filter

## Filter Parameters

$\mathrm{F}_{\mathrm{s}}=$ Sample rate in Hz
$\mathrm{F}_{\mathrm{c}}=$ Cut frequency in Hz
HL=LR Filter type (high, low)
$Q=$ Filter $Q\left(s^{2}+\frac{w c}{Q} \times s+w c^{2}\right)$

## Error Checking

$0 \leq F_{c} \leq \frac{F_{s}}{2}$
$0 \leq F_{s} \leq 192 K$
$H L=(h i g h, l o w)$
$0 \leq Q \leq 100$


Figure 7. Second order variable $Q$ filter $\left(F_{c}=1200 H z, Q=1, H L=l o w\right)$

## Equation

$$
\begin{aligned}
& \left.\begin{array}{l}
w c=2 \times \pi \times F_{c} \\
\text { if } H L(1: 3)==^{\prime} l o w^{\prime} \\
B a
\end{array}\right]\left[\begin{array}{lll}
0 & 0 & w c^{2}
\end{array}\right] \\
& A a=\left[\begin{array}{ll}
1 & \frac{w c}{Q} w c^{2}
\end{array}\right] \\
& \text { else } \\
& B a=\left[\begin{array}{lll}
1 & 0 & 0
\end{array}\right] \\
& A a=\left[\begin{array}{lll}
1 & \frac{w c}{Q} w c^{2}
\end{array}\right] \\
& \text { end } \\
& k=2 \times \pi \times \frac{F_{c}}{\tan \left(\pi \times \frac{F_{c}}{F_{s}}\right)} \\
& B=\left[B a(1) \times k^{2}+B a(3)+B a(2) \times k,-2 \times B a(1) \times k^{2}+2 \times B a(3),-B a(2) \times k+B a(1) \times k^{2}+B a(3)\right] \\
& A=\left[A a(1) \times k^{2}+A a(3)+A a(2) \times k,-2 \times A a(1) \times k^{2}+2 \times A a(3),-A a(2) \times k+A a(1) \times k^{2}+A a(3)\right]
\end{aligned}
$$

## Filter Coefficients

$B=\frac{B}{A(1)}$
$A=\frac{A}{A(1)}$

### 1.8 Second order Butterworth Filter from Variable Q

Second order Butterworth filter can be realized by using variable $Q$ filter with $Q=0.707$

### 1.9 Second order Bessel Filter from Variable Q

Second order Bessel filter can be realized by using variable $Q$ filter with $Q=0.5$

### 1.10 First Order Butterworth Filters

Filter Parameters
$\mathrm{F}_{\mathrm{s}}=$ Sample rate in Hz
$\mathrm{F}_{\mathrm{c}}=$ Cut frequency in Hz
HL=LR Filter type (high, low)

## Error Checking

$0 \leq F_{c} \leq \frac{F_{s}}{2}$
$0 \leq F_{s} \leq 192 \mathrm{~K}$
$H L=($ high,low $)$


Figure 8. First order Butterworth $\left(\mathrm{F}_{\mathrm{c}}=1200 \mathrm{~Hz}, \mathrm{HL}=\right.$ low $)$

## Equation

INSTRUMENTS

$$
\begin{aligned}
& k=\frac{2 \times \pi \times F_{c}}{\tan \left(\frac{\pi \times F_{c}}{F_{s}}\right)} \\
& W c=2 \times \pi \times F_{c} \\
& \text { If } H L(1: 3)=^{\prime} l o w^{\prime} \\
& b 0=\frac{W c}{k+W c} \\
& b 1=\frac{W c}{k+W c} \\
& \text { else } \\
& b 0=\frac{k}{k+W c} \\
& b 1=-\frac{k}{k+W c}
\end{aligned}
$$

end
$a 1=\frac{W c-k}{k+W c}$

## Filter Coefficients

$B=\left[\begin{array}{lll}b 0 & b 1 & 0\end{array}\right]$
$A=\left[\begin{array}{lll}1 & a l & 0\end{array}\right]$

### 1.11 Second order Chebychev

## Filter Parameters

$\mathrm{F}_{\mathrm{s}}=$ Sample rate in Hz
rip=Ripple specification in dB
typ=Filter type (high,low,stop)

```
if typ(1:3) == `sto'
Else
    Fc=Cutoff frequency in Hz
        If Scale peak to OdB
    If Scale PB to OdB
        if nrm\cong1
        rip = rip }\times-
        end
End
```


## Error Checking

$0 \leq F_{c} \leq \frac{F_{s}}{2}$
$0 \leq F_{s} \leq 192 K$
$0 \leq r i p \leq 10$
Nrm $=1,-1$
$H L=(h i g h, l o w$, stop $)$


Figure 9. Second order Chebychev ( $\mathrm{F}_{\mathrm{c}}=600 \mathrm{~Hz}$, typ=high, rip=3dB)

## Equation

If typ (1:3)=='sto'
Call cheby1 (ord, rip, $\frac{2 \times F_{c}}{F_{s}}$, HL)
else
Call $\operatorname{soCHBI}\left(\mathrm{F}_{\mathrm{c}}, \mathrm{F}_{\mathrm{s}}, \mathrm{rip}, \mathrm{HL}\right)$
End

Function soCHBI ( $\mathrm{F}_{\mathrm{c}}, \mathrm{F}_{\mathrm{s}}$, rip, HL$)$

$$
\begin{array}{ll}
\text { If sign (rip) } & >0 \\
\text { Else } & \text { Sf=1 } \\
& S f=0
\end{array}
$$

End
end
if $\operatorname{HL}(1: 3)==^{\prime} l o w^{\prime}$

$$
B a=\left[\begin{array}{lll}
0 & 0 & c \times w c^{2}
\end{array}\right]
$$

$$
A a=\left[\begin{array}{ccc}
1 & w c \times a & b \times w c^{2}
\end{array}\right]
$$

Else

$$
\begin{aligned}
& B a=\left[\begin{array}{lll}
\frac{c}{b} & 0 & 0
\end{array}\right] \\
& A a=\left[\begin{array}{lll}
1 & w c \times \frac{a}{b} & \frac{w c^{2}}{b}
\end{array}\right] \\
& \text { End }
\end{aligned}
$$

$$
\begin{aligned}
& R=\mid r i p \\
& \text { If } R==0 \\
& B=\left[\begin{array}{lll}
1 & 0 & 0
\end{array}\right] \\
& A=\left[\begin{array}{lll}
1 & 0 & 0
\end{array}\right] \\
& \text { else } \\
& w c=2 \times \pi \times F_{c} \\
& \varepsilon=\sqrt{10^{\frac{R}{10}}-1} \\
& \alpha=\frac{a \sinh \left(\frac{1}{\varepsilon}\right)}{2} \\
& \beta 1=3 \times \frac{\pi}{4} \\
& \beta 2=5 \times \frac{\pi}{4} \\
& s 1=\sinh (\alpha) \times \cos (\beta 1)+\cosh (\alpha) \times \sin (\beta 1) \times i \\
& s 2=\sinh (\alpha) \times \cos (\beta 2)+\cosh (\alpha) \times \sin (\beta 2) \times i \\
& a=\operatorname{real}(s 1+s 2) \\
& b=\operatorname{real}(s 1 \times s 2) \\
& c=b \\
& \text { if } s f \\
& c=\frac{c}{\sqrt{1+\varepsilon^{2}}}
\end{aligned}
$$

$$
\begin{aligned}
k & =2 \times \pi \times \frac{F_{c}}{\tan \left(\pi \times \frac{F_{c}}{F_{s}}\right)} \\
B & =\left[B a(1) \times k^{2}+B a(3)+B a(2) \times k,-2 \times B a(1) \times k^{2}+2 \times B a(3),-B a(2) \times k+B a(1) \times k^{2}+B a(3)\right] \\
A & =\left[A a(1) \times k^{2}+A a(3)+A a(2) \times k,-2 \times A a(1) \times k^{2}+2 \times A a(3),-A a(2) \times k+A a(1) \times k^{2}+A a(3)\right] \\
B & =\frac{B}{A(1)} \\
A & =\frac{A}{A(1)}
\end{aligned}
$$

End

## 2 Number representation format for filter coefficients

AIC codecs comes in two flavors. The "standard" version of the MiniDSP uses a 16 bit coefficient and a 24 bit data word for miniDSP_A and 28 bit data word for miniDSP_D while the "enhanced" version of the MiniDSP uses a 24 bit coefficient and a 32 bit data word. The AIC3254 and AIC3204 are enhanced devices. The TSC2117, AIC36, AC3110, AIC3111, and AIC3120 are standard devices.

All of the AIC codec devices use a 3.x data format ( 3.21 for the standard devices and 3.29 for the enhanced devices). This permits only two magnitude bits of headroom for signals that are greater then 1. To reduce the chance of clipping the signal in the AIC devices, the overall gain of the filter is moderated by scaling the numerator value based upon the value of the b0 term.

The coefficient size in the AIC codec family is 16 bit 1.15 format for the standard devices and a 24 bit 1.23 format for the enhanced AIC devices. With these formats the MiniDSP coefficients are able to represent a maximum positive gain of $1-2^{-15}$ for a 16 bit coefficient and $1-2^{-23}$ for a 24 bit coefficient. When filter coefficients are computed for an AIC codec, the gain of the filter response is scaled to permit the values to be represented in a 1.23 or a 1.15 format.

Once we have computed the filter equations from above we then must perform a couple of steps prior to loading the coefficients into the codec.

In the AIC codecs use a specific biquad implementation to accommodate the 1.15 and 1.23 coefficient data format.

$$
y(n)=b_{0} \times x(n)+2 \times b_{1} \times x(n-1)+b_{2} \times x(n-2)+2 a_{1} \times y(n-1)+a_{2} \times y(n-2)
$$

1. For format we first must scale the $b$ terms by the b0 value. The b0, b1, and b2 terms are multiplied by a scaling value to limit the overall gain of the filter.

- If b0 is greater than 1 , then the default value for the scaling value is $1 / b 0$, otherwise it is 1
- The scaling factor is then applied to the b0, b1, and b2 terms of the filter.
- This default value is computed and displayed in a user modifiable field when the filter coefficients are computed.
- The user is permitted to change this value to a smaller value. However if they attempt it set it to a larger value than the default scaling value then the value will snap to the default scaling value.

2. Then both the numerator and denominator coefficients are scaled by a constant value

- If the coefficients are being computed for a "standard" device then

The b0, b1, b2, a1, and a2 terms are multiplied by $2^{15}$ and rounded to integer

- If the coefficients are being computed for an "enhanced" device then

The b0, b1, b2, a1, and a2 terms are multiplied by $2^{23}$ and rounded to integer.
3. Then we scale the b1 and a1 terms by 0.5 .

Appendix A illustrates the generation of coefficients using the above procedure.

### 2.1 Filter coefficient normalization

Filter coefficient normalization is performed to limit the size of the coefficient values, as described above, and to limit the maximum gain of the filter to avoid clipping.

There are two places where clipping can occur.

1. Internal signal levels and clipping

The miniDSP is able to internally represent a data value using a 3.29 or 3.21 format. This permits signal levels as large as 12 dB to be represented. However, the intermediate gains inside of a filter can be higher than the signal levels that are visible at the output of a component. To account for this, filter gains are typically scaled to reserve part or all of this 12 dB as headroom for internal computations.
2. Output signal levels and clipping

The maximum signal level that can be output without clipping by the I2S output or the DAC interpolator is a data value represented as a by a 1.29 or 1.21 value ( 0.99 and -1.0 ). This corresponds to a signal level of 0 dB .

Coefficient scaling can be used to avoid clipping during internal operations and when the signal is sent to the $\mathrm{I}^{2} \mathrm{~S}$ or interpolator outputs.

For example, we wish to use an EQ filter that has a gain of 15 dB at 500 Hz . This filter response is shown as the blue curve in Figure 10. To avoid overflow for our internal representation, we normalized the filter coefficients so that the signal that is output does not exceed 5 dB . In this example, the filter gain is scaled by 10 dB (multiplying the coefficients by 0.316227766 ). The scaled filter response is shown by the red curve in Figure 10.

Similarly to avoid clipping when the signal was output, the filter gain should be scaled so that it does not exceed 0 dB . In this example, the filter gain is scaled by 15 dB (multiplying the coefficients by $0.177827941)$.. This is shown by the green curve in Figure 10.


Figure 10. Normalizing filter response

## 3 Updating the codec filter coefficients

A host controller needs to provide the filter coefficient values over I2C to the AIC codecs. On the controller, the coefficient values need to be pre computed and stored in a table. The host controller will read the values from the table and download the coefficient values in a sequence that starts at the current biquad filter setting to the desired new value when an update is requested. The change of gains must be in increments/decrements of $1 / 4 \mathrm{~dB}$ to avoid pops and clicks. For instance, if an EQ filter at 200 Hz needs to be operated between ranges of -8 dB to 8 dB , the host controller needs to maintain a table of b0, b1, b2, a1 and a2 terms through -8db, $7.75 \mathrm{~dB},-7.5 \mathrm{~dB} . . .7 \mathrm{~dB}, 7.25 \mathrm{~dB}, 7.5 \mathrm{~dB}, 7.75 \mathrm{~dB}, 8 \mathrm{~dB}$.

Table 1. EQ Filter coefficients table in host controller for "enhanced" codecs

|  | b0 | b1 | b0 | a1 | a2 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| -8 dB | 0x7F5119 | $0 \times 812 \mathrm{FC} 5$ | $0 \times 7 \mathrm{E} 69 \mathrm{BC}$ | $0 \times 7 \mathrm{ED} 03 \mathrm{~B}$ | $0 \times 82452 \mathrm{~A}$ |
| -7.75 dB |  |  |  |  |  |
| -7.5 dB |  |  |  |  |  |
| -7.25 dB |  |  |  |  |  |
| $\ldots$ |  |  |  | 0 | 0 |
| 0 dB |  | 0 |  |  |  |
| $\ldots$ |  |  |  |  |  |
| 7.5 dB |  |  |  |  |  |
| 7.75 dB |  |  |  |  |  |
| 8 dB |  | $0 \times 7 \mathrm{~F} 6664$ | 0x81C7F3 | 0x7D23F5 | 0x7F7E70 |

## Appendix A. Biquad coefficients computation example

This appendix illustrates the computation biquad coefficients and converting them into format required to load in AIC codecs.

1. Filter Specification: $E Q$ filter with $F_{c}=5000 \mathrm{~Hz}$, Gain $=6 \mathrm{~dB}$ and $\mathrm{Q}=2.87(\mathrm{BW}=1742 \mathrm{~Hz})$ on AIC3254.

Applying the equations in section 1.2 we get the biquad coefficients as
$b 0=1.03381744095486$
$b 1=-1.85413395878212$
$b 2=0.898225719031722$
$a 1=1.85413395878212$
$a 2=-0.932043159986584$
Before writing these coefficients to codec memory, couple of normalization steps must be performed based on their values according to section 2.
2. Since $\mathrm{b} 0>1$, we need to scale the numerator coefficients by scale factor $\frac{1}{b 0}$
$b 0=0.992464542388916015625$
b1 $=-1.77996826171875$
b2 $=0.862296581268310546875$
3. Scale the b1 and a1 by 0.5 .

$$
\begin{aligned}
& b 0=0.992464542388916015625 \\
& \mathrm{~b} 1=-0.889984130859375 \\
& \mathrm{~b} 2=0.862296581268310546875 \\
& \mathrm{a} 1=0.92706697939106 \\
& \mathrm{a} 2=-0.932043159986584
\end{aligned}
$$

4. Since the coefficients are to be computed for 'enhanced' device, we need to scale it by $2^{23}$ and rounded to nearest integer. Hence the final coefficient hexadecimal values that has to be loaded onto the AIC3254 are

$$
\begin{aligned}
& b 0=0 \times 7 \mathrm{~F} 0914 \\
& \mathrm{~b} 1=0 \times 8 \mathrm{E} 1500 \\
& \mathrm{~b} 2=0 \times 6 \mathrm{E} 5 \mathrm{FBC} \\
& \mathrm{a} 1=0 \times 76 \mathrm{AA} 20 \\
& \mathrm{a} 2=0 \times 88 \mathrm{~B} 2 \mathrm{D} 1
\end{aligned}
$$

