



Generic RLC high-pass filter as simple geophone model.

$$\text{Transfer function} = \frac{V_{out}}{V_i} = \frac{s^2}{s^2 + \frac{1}{R_L C} s + \frac{1}{LC}} = \frac{s^2}{s^2 + 2\xi\omega_n s + \omega_n^2}$$

$$\omega_n = \frac{1}{\sqrt{LC}}$$

$$2\xi\omega_n = \frac{1}{R_L C} \Rightarrow \xi = \frac{1}{2R_L} \sqrt{\frac{L}{C}}$$

From Encyclopedia of Petroleum Science & Engineering V3
Geophone equivalent circuit values:

$$B = \text{geophone open-circuit physical damping} \left[\frac{\text{dyne}}{\text{cm/s}} \right]$$

$$K = \text{geophone spring constant} \left[\frac{\text{dyne}}{\text{cm}} \right]$$

$$M = \text{geophone mass} [\text{Kg}]$$

$$G = \text{geophone sensitivity} \left[\frac{\text{V}}{\text{cm/s}} \right]$$

$$F_0 = \text{geophone natural frequency} [\text{Hz}]$$

$D = \text{geophone open-circuit damping ratio versus critical damping}$

$$R_C = \text{geophone coil resistance} [\Omega]$$

$$L_C = \text{geophone coil inductance} [H]$$

M, G, F_0, D, R_C are usually provided by geophone datasheet

Since K and B are usually not provided on geophone spec. sheets we must calculate them from other parameters which are available.

$$2\pi F_0 = \sqrt{\frac{K}{M}} \Rightarrow K = \frac{M}{(2\pi F_0)^2}$$

$$B = 2\omega_0 M D = 4\pi F_0 M D$$

$$R_{eqv} = \frac{G^2}{4\pi F_0 MD} [\Omega]$$

$$L_{eqv} = \frac{G^2}{4\pi^2 F_0^2 M} [H]$$

$$C_{eqv} = \frac{M}{G^2} [F]$$

Geophone PS-4.5B datasheet:

Natural frequency [Hz] = $4.5 \pm 10\%$

Typical open-circuit damping = 0.6

Coil resistance [Ω] = $375 \pm 5\%$

Moving mass [g] = 11.3

Sensitivity [V/cm/s] = 28.8

$$K = \frac{11.3e-03}{(2\pi 4.5)^2} = 14.1349e-06 \left[\frac{dyne}{cm} \right]$$

$$B = 2\omega_0 MD = 4 \cdot \pi \cdot 4.5 \cdot 11.3e-03 \cdot 0.6 = 38.34e-02 \left[\frac{dyne}{cm/s} \right]$$

$$R_{eqv} = 2163.38 [\Omega]$$

$$L_{eqv} = 91.82 [H]$$

$$C_{eqv} = 13.62e-06 [F]$$

Now, let's take a look to SM-24 geophone:

Natural frequency [Hz] = $10.0 \pm 2.5\%$

Typical open-circuit damping = 0.25

Coil resistance [Ω] = $375 \pm 2.5\%$

Moving mass [g] = 11

Sensitivity [V/cm/s] = $28.8 \pm 2.5\%$

Typical damping (@ $R_s = 1339\Omega$) = 0.60

Typical damping (@ $R_s = 1000\Omega$) = 0.69

In open-circuit we got following parameters:

$$K = 2.786e-06 \left[\frac{\text{dyne}}{\text{cm}} \right]$$

$$B = 34.558e-02 \left[\frac{\text{dyne}}{\text{cm/s}} \right]$$

$$R_{eqv} = 2400 [\Omega]$$

$$L_{eqv} = 19.1 [H]$$

$$C_{eqv} = 13.26e-06 [F]$$

$$G = \text{still } 28.8 \left[\frac{\text{V}}{\text{cm/s}} \right]$$

Transfer function becomes:

$$\xi = \frac{1}{2R_{eqv}} \sqrt{\frac{L_{eqv}}{C_{eqv}}} = 0.25 \quad (\text{obviously})$$

$$\omega_n = \frac{1}{\sqrt{L_{eqv} \cdot C_{eqv}}} = 62.832 \left[\frac{\text{rad}}{\text{s}} \right]$$

$$\text{Out}(s) = \frac{28.8s^2}{s^2 + 31.42 \cdot s + 3947.84} \quad (\text{no shunt resistor})$$

Ok, geophone response changes upon shunt resistor so let's take care of shunt resistor (in this case we don't take care of coil's inductance):

$$R_{load} = R_{coil} + R_{shunt} \quad \text{this resistor is in parallel to} \quad L_{eqv}' = 19.1 [H]$$

$$R_{eqv}' = R_{eqv} || R_{load} = \frac{R_{eqv} \cdot R_{load}}{R_{eqv} + R_{load}}$$

That's why we get different damping value for different shunt resistors.

Since shunt resistor acts as resistive partitor, it changes also sensitivity:

$$G' = G \frac{R_{shunt}}{R_{coil} + R_{shunt}}$$

Then we have new equivalent system:

$$Out(s) = \frac{22.5s^2}{s^2 + 79.18 \cdot s + 3947.84} \quad (R_{shunt} = 1339)$$

$$Out(s) = \frac{20.9s^2}{s^2 + 90.02 \cdot s + 3947.84} \quad (R_{shunt} = 1000)$$

Geophone SM-24 response curve (shunt resistor – damping)

