

The SD16_A as a thermal random number-generator
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The SD16_A analog-to-digital converter module, implemented in some members of the Texas Instruments MSP430 microcontroller line, can function as a surprisingly good source of randomly generated bytes, producing them at the rate of four per millisecond. The randomness can be traced to a fundamentally thermal source, so this is a truly random generator, not a pseudo-random one.

What to do

Configure the SD16_A for maximum gain, input 7 (shorted), and an oversampling ratio of at least 256. (Smaller may do in some cases - see below). Set the input clock divider to make a 1MHz converter clock and set the LSBACC bit to give access to the low order part of the converter's filter register.

When running with a 16MHZ MCLK, C code to accomplish this would be (assuming an appropriate header file that defines the symbols the same way the User's guide does):

```
//1 MHz, (MCLK/16), turn reference generator on.
SD16CTL = SD16XDIV_2 + SD16DIV_0+ SD16SSEL_0 + SD16REFON;
// Oversampling ratio set to 256, enable LSB access, no interrupts,
SD16CCTL0 = SD16OSR_256 + SD16LSBACC;
// Gain = 32 (actually 28), channel is 7 (shorted)
SD16INCTL0 = SD16GAIN_32 + SD16INCH_7;
// Now Go
SD16CCTL0 |= SD16SC;
```

After each conversion, the SC16IFG flag will set in the SD16CCTL0 register. If you have the interrupt enabled (by setting SD16IE in that same register) the module will post an interrupt. When the flag sets, the lower byte of the SD16MEM0 result register contains your new randomly generated byte. Reading that byte will reset the flag bit. At this clock rate and OSR value, the flag bit will set again with a new randomly-generated byte every 256 μ seconds. To access it in C, assign the value in SD16MEM0 to a variable of type unsigned char.

This recipe assumes that the SD16_A is used for no other purpose. In fact it can be shared with another use, and configured as a random generator only when needed or when it is free from other demands. Even when doing its intended job as an ADC for nonzero signals, it will also be generating a noisy byte in the bottom of its output register as a result of each conversion. If it is run with high gain and an OSR of at least 256, and if the signal being converted lies safely within its input range limits, one would expect that the low order byte would be much like it is during dedicated operation. We have not investigated the quality of that byte in such conditions, but you may find it usable.

As discussed below, you can probably also get away with an oversampling ratio as small as 128, but there is less theory available to tell you why you should trust it then.

If all you want is a recipe, there it is.

How well it works

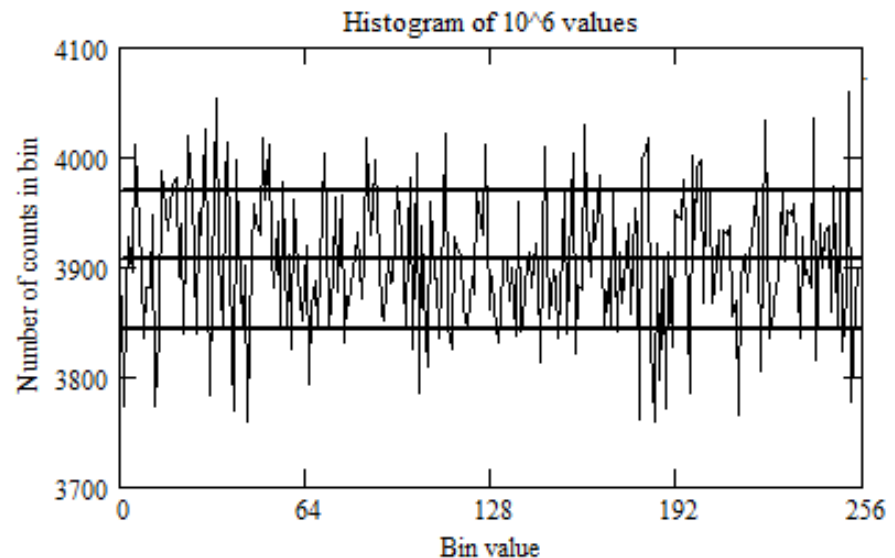
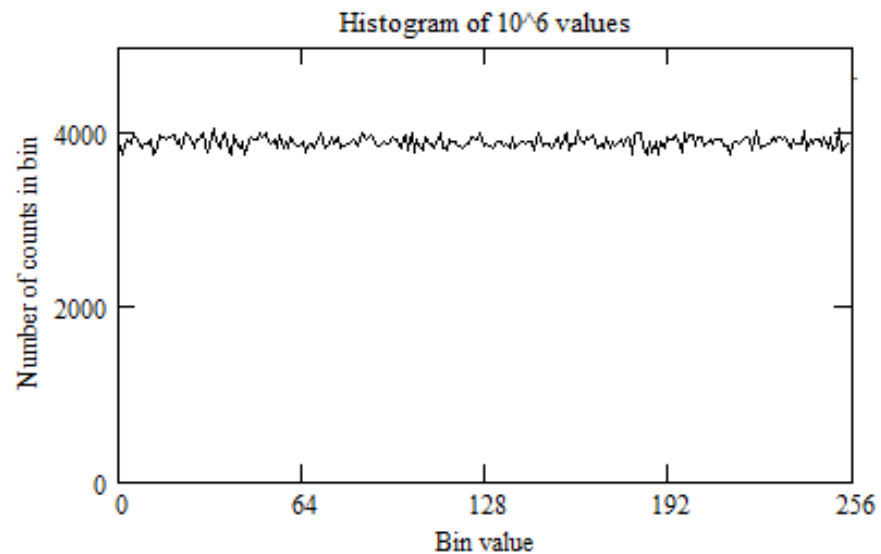
If we are trying to make a number generator with a uniform distribution, one that produces all possible values with equal probability, we ought to check its output to see that all values really are produced about equally often. If we want the generator's past history to offer no clues about its future actions, we ought to check the autocorrelation function of the byte sequence to make sure that a large byte value is not, for instance, usually followed by a small one or vice versa. As will be argued in the appendix, these are necessary but not sufficient tests for randomness.

To run these tests, we need a file of output bytes from our generator. There is a program in the appendix which when loaded into the target board of an eZ430_2013 evaluation kit sends out bytes in start-stop serial form (for receipt by a UART) that have been randomly generated by the SD16_A in the manner described above. It uses the Timer_a module to

simulate a serial communication port and runs at 115.2KBaud with its output on P1.1. We removed the target board from the USB stick hardware of that evaluation kit, attached a serial-to-USB interface cable from FTDI, and read the byte stream into a PC for further processing.

The results of these two tests on a sample of $N=10^6$ bytes generated in this manner are shown in the figures at the right.

The first figure shows a histogram of values observed in the record, accumulated by setting up 256 counters (the "bins"), one for each possible byte value, scanning the record, and for each value observed incrementing the corresponding bin. The second figure is an expanded version with three heavy black lines indicating the average n and the average plus and minus the expected standard deviation $n \pm \sqrt{n}$. The average number in each bin is $n = N / 256 = 10^6 / 256 = 3906.25$.



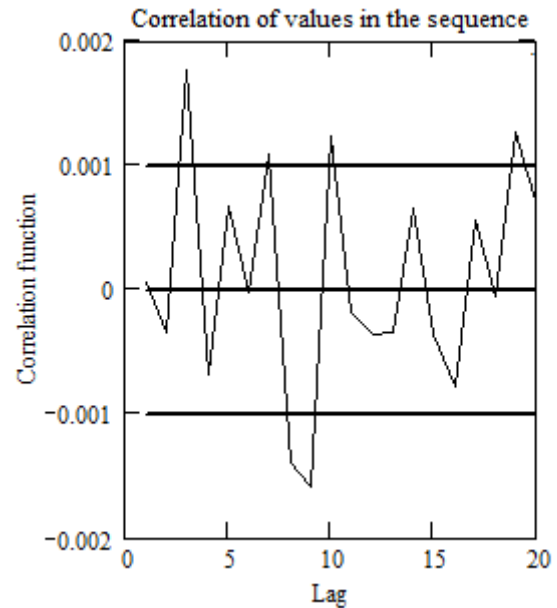
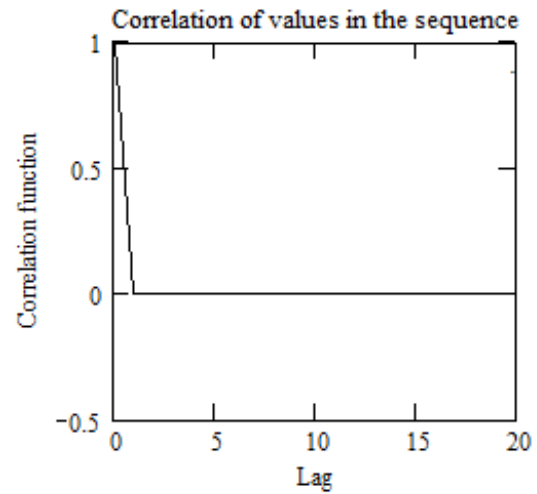
The next two figures show the results of an autocorrelation calculation based on the same data record for lags between 0 and 20. (See the appendix for details of the calculation.) The first figure includes for comparison the correlation at zero lag, which is by definition 1.

The second figure expands the scale for the remaining values and shows for comparison two horizontal lines at $\pm 1/\sqrt{N} = \pm 0.001$ indicating the expected standard deviation of the results for uniformly distributed randomly-generated values.

The TI user's manual text and figures describing the SD16 makes it clear that the value of the converted number does not settle in a single conversion cycle, and that for two cycles after an input value changes there is a significant error in the most significant bits of the ADC result. The new value remains correlated with the previous value. We would not expect this correlation to occur with constant input and in the noisy lower bits, and the results shown here confirm that indeed it does not. Successive bytes in the sequence are effectively uncorrelated.

A stream of uncorrelated symbols, each occurring with probability p_i , has a Shannon entropy in bits per symbol defined by $S = -\sum_i p_i \cdot \log_2(p_i)$, where the summation index i runs over all symbols. In our case, $0 \leq i \leq 255$. For a theoretically perfect generator, all the probabilities would be $p_i = 1/256$, $-\log_2(p_i) = 8$, and $S=8$.

We can approximate the probability of seeing a byte of value i by the relative frequency of occurrence of that value in our test sequence. With a finite sequence, the bin contents will of course not be exactly equal and not exactly equal to the underlying probability so we do not expect the resulting estimate to be exactly $S=8$, but with a large sample such as the one we have, we expect to be close. To make that estimate we take $p_i \approx n_i/N$ where n_i is the number of counts in the i -th bin (as plotted in the first two figures of this section) and N is the total length of the sample, $N = \sum_{i=0}^{255} n_i$. Estimating S in this way gives $S \approx 7.99981$ bits/symbol. We will not be far wrong to call that 8 bits of entropy per generated byte.



The appendix contains a pointer to a suite of tests offered by NIST for candidate random number generators, and to the “Dieharder” test suite, a more convenient implementation of those tests along with several others.

It also contains some rude words about the ability of any test to actually confirm true randomness. Still, if we have a supposedly random generator of numbers, it ought to be able to pass those tests, as the appendix argues they should, most of the time. When we ran the STS suite on the same file of 10^6 randomly generated bytes tested above it passed all tests successfully. The result file is in the last appendix.

Why it works at all

Every time a capacitor is connected to a resistive source, allowed to settle, and then disconnected it acquires a randomly generated voltage with standard deviation $V_{RMS} = \sqrt{kT/C}$ in addition to whatever voltage the source is intentionally providing. This random addition is called “contact noise”, but it is actually the resistor that is noisy, not the contact, as explained in the appendix. Here k is Boltzmann’s constant and T is the absolute temperature, so at room temperature this becomes $V_{RMS} = 64\mu V / \sqrt{C}$ for C in picofarads.

Every microsecond when the input sampler of the SD16_A contacts the external circuit and the voltage on its 20pF sampling capacitor settles to a new measurement of the nominally zero input value, that value is zero plus or minus “contact noise” that has a standard deviation of $64/\sqrt{20} = 14$ microvolts. That voltage is amplified by a factor of 28, so will have a standard deviation of 0.4mV, and applied to the sigma-delta modulator. In the course of the conversion, 256 of these values will be more-or-less averaged by the digital filter, to yield a random contribution no smaller than $400/\sqrt{256} \approx 25\mu V$. This truly-random contribution could approach that theoretically smallest value if the filter simply averaged. In fact it does something more complicated to minimize the shaped quantization noise of the second order delta modulator, so we expect that there will be more of the truly random noise than this minimum. For OSR = 256, the most significant bit of the output register is bit 23 (see figure 26-5 of the MSP430F2xxx User’s guide, SLAU144J), and that bit is worth 600 mV. The least significant bit of the register is therefore worth $2^{-23} * 600 \text{ mV} \approx 72\text{nV}$. That means the $25\mu V$ noise contribution is worth at least $25\mu V / 72\text{nV} = 350$ LSB, and we expect it to be Gaussian noise, distributed along the familiar bell-shaped curve of probability density.

The simple treatment in the paragraph above requires some assumptions about just how the input amplifier and delta modulator are constructed and operated. Based on the gain and capacitance specifications and the fact that the module still offers gain when the active amplifiers are omitted, I have assumed that each of the two C_s capacitors (10pF at gain 32) in figure 26-2 of the F2xx users guide (SLAU144J) is made of eight 1.25pF capacitors (like the one that is used at gain 1) that are charged in parallel and then connected in series when presented to the ADC core. A final factor-of-four gain is achieved some other way, perhaps in the delta modulator, or perhaps by actually splitting each of the 1.25pF capacitors four ways. There are other ways that the input amplifier could be operating, but most of them lead to the same noise estimate. None we have thought of leads to a smaller one.

As we will see, the output is actually noisier than this estimate would lead us to expect, but that’s more-or-less OK even though it is not quite clear just where that is all coming from. We can guess that it is quantizing noise which will be pretty well randomized by the presence of the contact noise, but we only need a guarantee of enough thermal noise to make things genuinely random, to fill up the lower byte with “good” noise known to originate in a thermal source that we expect to have a Gaussian distribution.

To check on this noise estimate, a program was written for the eZ430F2013 that accumulated statistics on the SD16_A output in the upper (normally used) section of the SD16 output register. For comparison, we need a

prediction based on our noise model above for what we should expect. The MSB of the upper output register is worth 600mV at Gain=1, so its LSB is worth $600\text{mV} \cdot 2^{-15} = 18\mu\text{V}$. At any other gain it is worth $18\mu\text{V}/G$. Our simple model of the filter effect is that it will simply average the noise samples, so we expect them to be attenuated by a factor of $1/\sqrt{\text{OSR}}$. Thus we predict a noise in the upper register equal to

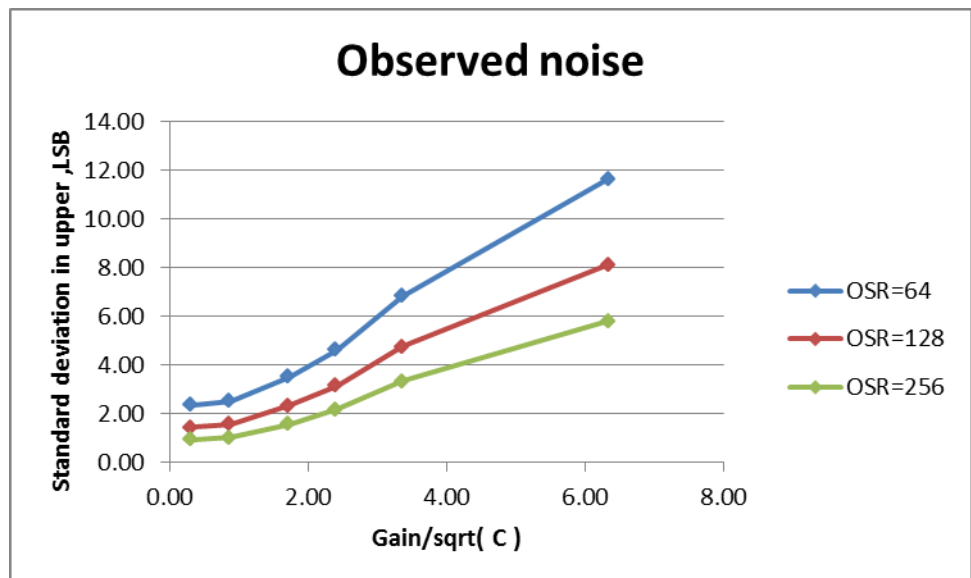
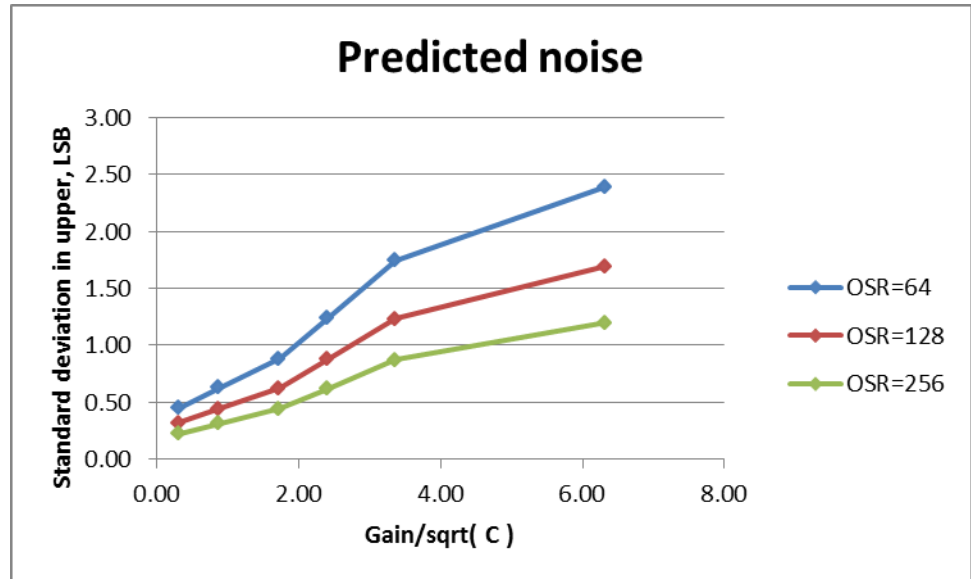
$$\frac{64\mu\text{V}}{\sqrt{C}} \frac{G}{18\mu\text{V}} \frac{1}{\sqrt{\text{OSR}}} = 3.6 \frac{G}{\sqrt{\text{OSR} \cdot C}} \text{ LSB.}$$

Plotting this out vs.

$G/\sqrt{C}$ for the various available gain settings (tick marks on the traces) and interesting values of OSR, we obtain the figure on the right.

Running a program in an eZ430F2013 to calculate the mean and standard deviation of 10^6 conversions for each of those cases gives instead the next figure. It has approximately the same shape, but the measured values are about four times larger than the predicted ones. If we knew where all that came from and how securely it was tied to a thermal source, perhaps we could confidently use a smaller OSR and generate bytes more rapidly. As things stand, this note recommends OSR=256.

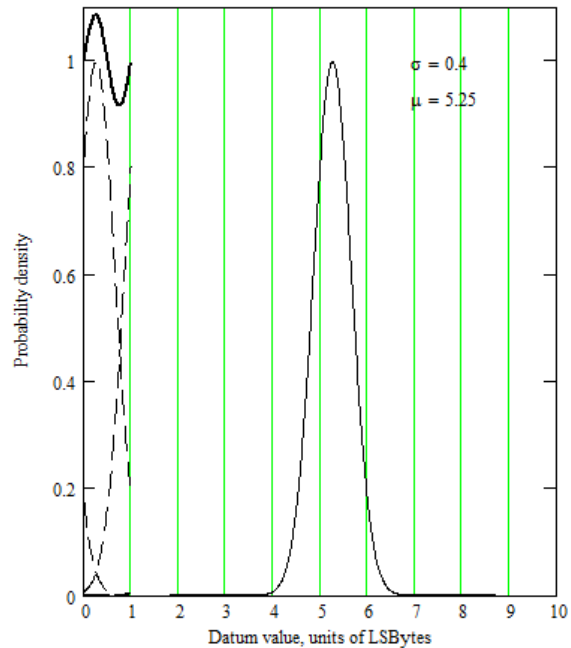
One of the authors' major goals in writing this note is to lure some of the SD16 design team into commenting on this comparison and revising the previous several paragraphs – all in aid of making more secure the theoretical foundations of the scheme and perhaps making it faster by leaving us more comfortable with smaller values of OSR.



Why it works so well

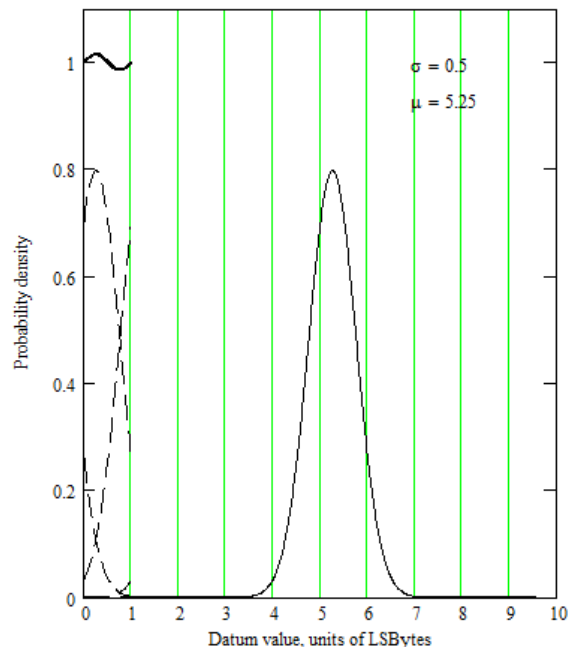
When you have a set of data with a Gaussian distribution and you take those numbers modulo something comparable with or smaller than their standard deviation, the result always comes out to be nearly uniformly distributed. That is the real key; if you have enough Gaussian noise to fill your byte, you don't care about much else. The rest of this section will show how that works.

In the example at the right, we see some graphs illustrating how that begins to take effect, where in these graphs we are taking things modulo 1. In our present application we can think of that unit 1 as being one byte; in our hardware the numbers are taken modulo 256. In the first figure the standard deviation of the Gaussian is less than half a byte – still a bit small – but when you take the ordinate of the curve modulo 1, that is when you slice it along each of the vertical green lines, superimpose those slices, and add them up as has been done with the dashed lines on the left side of the graph, you get a sum (heavy black line) that is not yet flat, but already has sharply limited variation. In this illustration the mean of the original distribution has been chosen $\frac{1}{4}$ unit off-center to cause the maximum possible variation in the black trace.

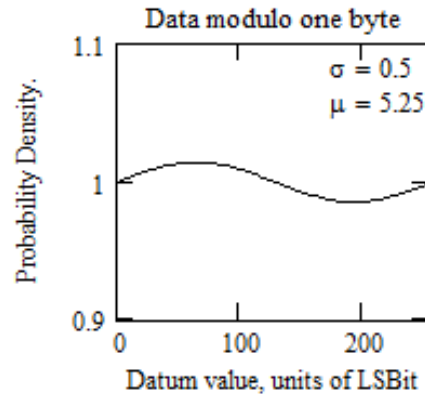
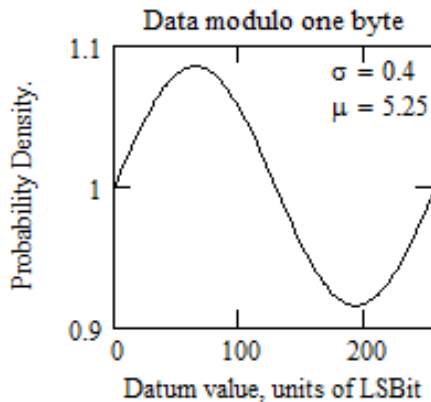


Well, how about adding a little more noise? When the Gaussian is only 20% wider, the variations in the heavy black trace shrink markedly. Let's plot that black trace separately, and follow its behavior as we increase σ (and thereby increase the width of the Gaussian) by a few more steps.

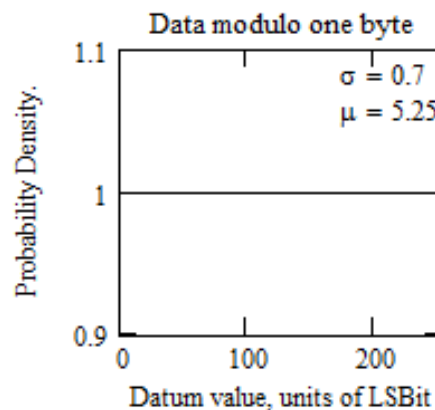
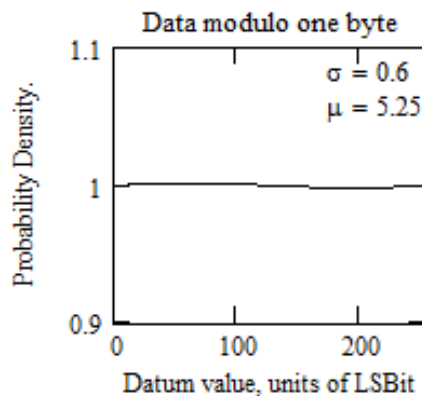
In these graphs below we have shown the X-axis scale in LSB, 0 to 255, replacing the scale of 0 to 1 bytes, now that we do not have to also show the Gaussian peak. The values of μ and σ are still shown in bytes for compactness and would have to be multiplied by 256 to get the corresponding values in LSB.



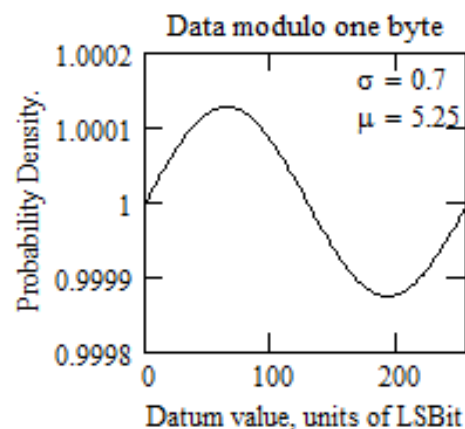
The first two graphs represent the two cases shown in full above.



As the standard deviation increases, the probability density rapidly flattens out until its variation becomes completely invisible when plotted at the original scale.



Now plotting that last case again but allowing the vertical scale to adjust we see that the shape of the variation has not changed, but that its scale has become so small as to be undetectable in practice. To get that degree of flatness takes a standard deviation of 0.7 times the modulus value. For data taken modulo one byte, that requires 180 LSB of noise standard deviation. More noise is better, so long as it all stays within the input range of the ADC; our OSB=256 case, with a contact noise contribution of 350LSB, is safe by a wide margin.



But there is additional value to an extremely flat distribution made by folding up a Gaussian as we have done above; you can't easily disturb it by adding something else to it. Adding something to the input of the ADC just moves the mean of the input Gaussian distribution. But when the resulting output distribution is flat, then the location of the original Gaussian's peak no longer matters. All that moving the peak could ever do was to move the location and perhaps reduce the

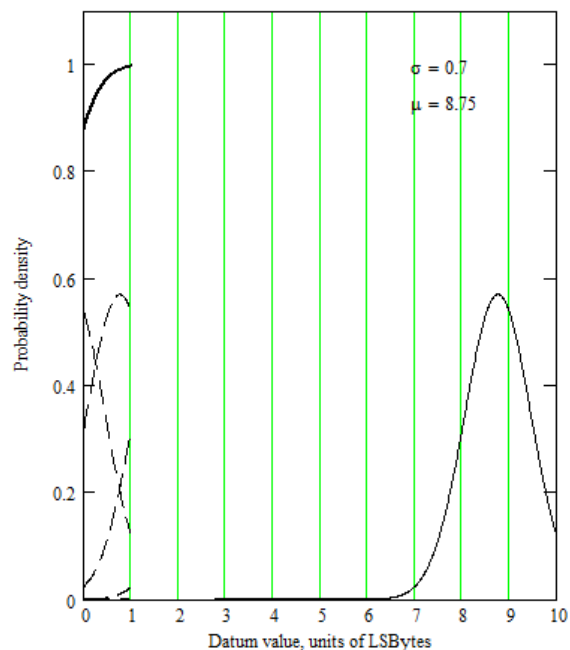
height of that wavy trace we have been watching. If the wave has a small enough amplitude to be undetectable, then the effect of a change in the mean of the noise is also undetectable.

That is the starting point for a useful way to think about other contributions to our noise generator's result. All that any additive (interfering) signal can do is to move that mean. If it moves the mean and leaves it in a new location, then quite clearly it has no effect on the performance of our generator. We won't see the same result of a conversion that we would have seen without the addition, but we will see another value drawn from the same nearly-flat distribution. It will be just as unpredictable, will be drawn from the same population of values and will have the same distribution. If the added signal moves the mean back and forth between conversions, we still won't have any way to tell that it has done so or any reason to wish that it hadn't. If it changes back and forth during a conversion, we expect that all it can do is to broaden the noise distribution, and as we can see that helps us out. Once we have enough Gaussian noise, it looks like we can relax about interference. So long as the SD16_A is well enough shielded to do its normal ADC function, it should be able to make high quality noise bytes.

So much for external noise sources. However the S-D modulator will respond to the input noise and its own quantization noise can become correlated with the contact noise. This possibility could take us into regions of sigma-delta converter design that we do not propose to enter. The contribution of an S-D designer would be welcome, but we will take it no farther, beyond noticing that this proposed use of the SD16A does appear to work remarkably well, so seems not greatly harmed by that possible effect.

It is worth noting that we do need the SD16_A to be working well as an ADC, and as already mentioned we need the entire input noise voltage range to fit within its linear input range. If one tail of the input noise gets outside the linear range of the ADC function, we can no longer guarantee a flat noise spectrum in the result, as illustrated in the plot at the right. The output value distribution in the case illustrated here has a distortion that is just the negative of the missing tail of the original distribution.

When the SD16_A is operating with its input range symmetric around zero, and with the input shorted as we do here, that requirement is easily met and the situation diagrammed here is easily avoided.



Conclusion

The SD16_A sigma-delta ADC can be operated as an excellent random generator of bytes, where the source of randomness can be traced to thermal noise.

Appendices

About Contact Noise

It is not actually the contact that is noisy.

Whenever you connect a warm resistor across a capacitor, the resistor generates Johnson (thermal) noise and applies it to the capacitor. Meanwhile the same resistor is discharging that capacitor. As the net result of those two actions, there is a random voltage appearing across the capacitor, which fluctuates as long as the resistor is connected. If the RC product is small, the range of frequencies involved may be very large and mostly outside the passband of a typical sensitive amplifier that may be looking at the capacitor. The amplifier may see nothing happening. When the resistor is disconnected from the capacitor, as happens every microsecond in the SD16_A, the voltage suddenly freezes at a definite value and can be seen by narrow-band circuitry. Since a new frozen value appears any time the capacitor is contacted long enough for a new equilibrium to be established, then disconnected, the effect has acquired the name contact noise even though the switch contact is not actually the source of the noise. The electrical resistance of the switch and circuit is the actual source, and what it contributes is thermal noise.

An electrical engineering text which analyzes this effect might proceed by integrating the Johnson noise spectrum over the bandwidth defined by the resistor and capacitor, considered as a single-section low-pass filter, and thereby could derive an expression for how much noise to expect. While it gives a nice picture of what is going on to anyone who already knows about Johnson noise, that approach is complicated; we won't do it that way.

A physicist looking at the same problem would more likely think about the Equipartition Theorem from Statistical Mechanics. It states (roughly) that any quadratic energy term in a system will have an average energy equal to $kT/2$ when the system is in thermal equilibrium. In our case, we notice that the voltage across a capacitor C gives rise to an energy term $\frac{1}{2} CV^2$ which is quadratic in V , its terminal voltage. We can set that term equal to $\frac{1}{2} kT$, then solve for the mean-squared terminal voltage $\langle V^2 \rangle = kT / C$.

At room temperature this becomes $V_{rms} = \sqrt{\langle V^2 \rangle} = \sqrt{kT/C} = 64\mu V / \sqrt{C}$ for C in picofarads, the result quoted in the body of the note. The 20pF input capacitor of the SD16_A will have a root-mean-square thermal noise voltage due to this effect of $64\mu V / \sqrt{20} = 14\mu V$.

About Random Numbers

There aren't any. However there are randomly generated numbers.

Once you have a number, however generated, it has a perfectly definite value and there is nothing random about it. The only thing that can be random about the situation is the way the number was generated. Said more compactly, a number cannot be random, but its value can be unexpected. For most purposes it is fair to call the process that generated it truly random if there is no way to predict (better than chance) the number that the generator is going to make next – even if you have full knowledge of the generator's history and internal state.

So it is fair to talk about random number-generators, but not random-number generators. Mostly, people are not careful about that distinction, but this note will try to be.

About Testing for Randomness

There is no good way to do it.

In the output from a perfectly random generator of numbers, at least one with a uniform distribution like we are trying to make here, all possible bit sequences are equally likely. A string of all ones or all zeros looks to us wildly non-random, but it is as likely as any other particular sequence in a random generator's output. In a single-byte result from the generator proposed here, you will see a solid zero about 15 times a second. You will see a pair of two zero bytes together more-or-less every 16 seconds, a trio of three in a row more or less every 72 minutes, four in a row about every twelve days, and so on. No particular sequence of the same length that you could name would be either more or less likely than one with all bits zero. You can't call any of them right or wrong, random or non-random in themselves.

What you can do is to test for properties that a large majority of randomly generated sequences is likely to have, realizing that any such test will sometimes call foul on a sequence that came out of a perfectly random generator. A truly random generator must eventually make all possible sequences – including all of those that fail your test. Also, there may also be chaotic sequences generated by a perfectly predictable (pseudo-random) process that always pass such a test, which a genuinely random generator could not always do.

In short, a generator that fails a sensible test consistently is with high probability not random. One that fails rarely may or may not be truly random. One that always passes is with high probability not truly random, though it may take an impractically long time to adequately explore “always”. So we can test for failed generators, but not for good ones.

We talked about two tests in some detail in the body of this note, based on the ideas that: 1) all possible byte values should occur about equally often and 2) pairs of bytes in sequence should be uncorrelated. These are relatively simple tests that are suggested by the physical process that we expect is going on in our generator. They characterize that process, which is believed to be fundamentally unpredictable, and they give these physicist writers a good feeling. They are also likely to catch a programing error should we make one. But they are not tests for randomness *per se*. Assurance of that has to come from knowledge of the underlying physics, and of the electronic and computational structure built atop that physics.

That said, there are some widely accepted tests that are thought to have relevance to cryptographic strength. A suite of them can be found at http://csrc.nist.gov/groups/ST/toolkit/rng/documentation_software.html. Any random generator of numbers that we want to take seriously ought to be able to pass them, at least most of the time (and that may be every time we have the patience to try). Again, as should be obvious from the fact that pseudo-random generators can also pass them, they are not tests for genuine randomness.

A more convenient implementation of some of these and other tests, ready to run on a Windows PC, can be found at <http://www.phy.duke.edu/~rgb/General/dieharder.php>

We have run the same 10^6 -byte sequence discussed above, produced by the generator proposed here through the NIST test suite using the supplied default values of the test parameters. The sequence passed all tests. (We did not successfully explore “always”.) The printout from those tests is included as the last appendix.

About Autocorrelation

The autocorrelation function of a sequence of values x_j at lag L is the averaged product of the deviations of x from its average μ , with the samples chosen L intervals apart, divided by the variance of the sequence. That is,

$$r(L) = \frac{\langle (x_{j-L} - \mu) \cdot (x_j - \mu) \rangle}{\langle (x_j - \mu) \cdot (x_j - \mu) \rangle}$$

The pointed brackets represent an average over a range of the index j large enough to be effectively infinite. If $L = 0$ we are calculating the correlation of each value of with itself; not surprisingly the numerator and denominator are equal in that case and answer comes out 1 for any sequence longer than L that has nonzero variance (so we don't end up dividing by zero). Any varying sequence is perfectly correlated with itself at zero lag.

For $L > 0$ we are asking whether variations from the average in one sample are mirrored in any way by the variations from average of the sample L time intervals later. If the sequence generator is purely random, the autocorrelation for any lag value $L > 0$ calculated over an infinite sample should be infinitely small.

But we do not have infinite sample sizes available, and when working with a small processor we may need to calculate a finite approximation to the autocorrelation efficiently. Paying attention to samples lost at the ends of the record and to the fact that the set of samples in the two factors are slightly different and may have slightly different averages, we recast the result above in terms of sums over a finite sample of size N as

$$\mu_A = \frac{1}{N-L} \sum_{j=1}^{N-L} x_j, \mu_B = \frac{1}{N-L} \sum_{j=L}^N x_j, C(L) = \left(\frac{1}{N-L} \right) \left[\sum_{j=L}^N (x_{j-L} - \mu_A) \cdot (x_j - \mu_B) \right] \text{ and finally}$$

$$r(L) = C(L) / C(0).$$

The expression for the Covariance $C(L)$ can be expanded and simplified as:

$$\begin{aligned} C(L) &= \left(\frac{1}{N-L} \right) \left[\sum_{j=L}^N (x_{j-L}) \cdot (x_j) - \mu_B \sum_{j=L}^N (x_{j-L} - \mu_A) - \mu_A \sum_{j=L}^N (x_j - \mu_B) + (N-L) \mu_B \mu_A \right] \\ &= \left(\frac{1}{N-L} \right) \left[\sum_{j=L}^N (x_{j-L}) \cdot (x_j) \right] - \mu_B \mu_A - \mu_B \mu_A + \mu_B \mu_A \\ &= \left(\frac{1}{N-L} \right) \left[\sum_{j=L}^N (x_{j-L}) \cdot (x_j) \right] - \mu_B \mu_A \end{aligned}$$

This simplification depends upon recognizing two of the sums in the first expansion as proportional to μ_A and μ_B . The final result expresses the result for $C(L)$ in terms of three sums that can be calculated together in a single pass over the data; the data record can be processed "on the fly" and never stored, so the calculation can be done in a processor with limited memory. With $C(L)$ in hand the autocorrelation is obtained as

$$r(L) = C(L) / C(0).$$

Autocorrelation values in the note were obtained by evaluating these expressions in that way.

Do note that the sum of products can be large when processing a large file. A random million-byte file will generate a sum of squares with a value approximately $128^2 \times 10^6 \approx 2^{34}$ that will overflow a four-byte field. The sum cannot be accumulated to adequate precision either as a 32-bit integer or in single precision floating point.

Program for the eZ430-F2013

The program below loaded into an eZ430-F2013 will send randomly generated bytes in start-stop serial format at 115.2 Kbaud out through P1.1, which is pin 3 of the MSP430F2013 processor included in the eZ430-F2013. The oversampling ratio may be changed by altering a statement just below the comment line // SD_16. However notice the warning message just above that line.

The program works as described in the text only for OSR $\geq$ 128. For smaller oversampling ratios, characters are produced faster than they can be sent, and successive characters in the serial communication output no longer represent successive characters in the generator output.

There are two separate files below, Main.c and Timer_A.c. They were compiled using IAR Embedded Workbench.

```
//Main.c
// Random Number generator test, target is MSP430F2013,
#include <msp430f2013.h>
int send_byte(char);
unsigned char Datum;
volatile unsigned int v = 0;

int main( void )
{
// Disable watchdog timer
WDTCTL = WDTPW + WDTHOLD;

// Set DCO to 16MHz, which is OK at 3.3V Vcc.
BCSCTL1 = CALBC1_16MHZ;
DCOCTL = CALDCO_16MHZ;

// Configure the ports
//P1
P1OUT = 0;    // Outputs are low
P1DIR = 0xFF; // All pins are output
P1SEL = BIT1; // And Bit1 is timer output.
//P2
P2OUT = 0;
P2DIR = 0;
P2REN = 0xFF;

// Timer_A
// P1.1 = data output Pin 3 of DIP package. (LED is P1.0, pin 2)
TACCR0 = 139;    // = 16 MHz/115.2 Kbaud
TACCTL0 = OUTMOD_1 + CCIE; // Set on event, enable interrupt;
TACTL = TASSEL_2 + ID_0 + MC_1;

// This SHIFT definition is the SD_16 register position from which the
// LSBit of the data byte is taken. SHIFT <= 8. Ordinarily 0 or 8.
```

```

#define SHIFT 0
// It and the oversampling ratio set below define the case.
// OSR >= 128 assumed so bytes are sent faster than they are produced.

// SD_16
//1 MHz, (MCLK/16), turn reference generator on.
SD16CTL = SD16XDIV_2 + SD16DIV_0 + SD16SSEL_0 + SD16REFON;
// Oversampling ratio set, enable LSB access, no interrupts,
SD16CCTL0 = SD16OSR_256 + SD16LSBACC;
// Gain = 32, channel is 7 (shorted)
SD16INCTL0 = SD16GAIN_32 + SD16INCH_7;
// Now Go
SD16CCTL0 |= SD16SC;

//*****
v = SD16MEM0; // Clear any leftover data.
//*****
__enable_interrupt();

// Event loop starts here
while(1)
{
// Wait for next value
while((SD16IFG & SD16CCTL0) == 0) v++;
// Shift during this assignment to move up the filter register.
Datum = SD16MEM0>>SHIFT;
send_byte(Datum);
} // End the event loop.

} // end main

```

```

// File Timer_A.c
#include <msp430f2013.h>
// Set TACCTL0 to one of these to either set or clear P1.1 on next event.
// Temporary reversal for test
#define SET  OUTMOD_1 + CCIE
#define RESET OUTMOD_5 + CCIE
enum {idle = 0, start, bit0, bit1, bit2, bit3, bit4, bit5, bit6, bit7, stop};
unsigned int serial_out_state = idle;
unsigned char Out;

// This routine called from main to initiate character output
// Return 0 for character accepted, 1 for refused (overflow).
int send_byte(char Outchar)
{
    if(serial_out_state == idle)
    {
        Out = Outchar;
        serial_out_state = start;
        return(0);
    }
    return(1); //Overflow error return
}

#pragma vector=TIMER_A0_VECTOR
__interrupt void Timer_A0( void )
{
    switch(serial_out_state)
    {
    case idle:
        {
            TACCTL0 = SET; // Set Idle line and wait for send_byte to be called.
            break;
        }

    case start:
        {
            TACCTL0 = RESET; // Make start bit
            serial_out_state = bit0;
            break;
        }

    // Send next bit of character.
    case bit0:
    case bit1:
    case bit2:
    case bit3:
    case bit4:
    case bit5:
    case bit6:

```

```
case bit7:
{
    if((Out&0x01) == 0) TACCTL0 = SET; // if bit is 0, output is 1
    else                TACCTL0 = RESET; // and vice versa.
    Out=Out>>1;          // shift to next bit
    serial_out_state++;   // increment to next state.
    break;
}
case stop:
{
    TACCTL0 = SET; // Set Idle line and
    serial_out_state = idle; // go to idle state.
    break;
}
default:
{
    serial_out_state = idle;
    break;
}
} //End switch(serial_out_state)
} //End __interrupt void Timer_A0( void )
```

Results of The NIST STS suite

These tests were performed running the STS test suite with the default parameters supplied by NIST.

STS Run
06 December 2013
RKG

Notes:

- 1) The data file, *ekstrom.raw*, is a file of 10^6 random bytes captured from a CPU configured to stream randomly generated numbers generated by the SD_16A in the processor of the EZ430F2013, using the program given in the previous section.
- 2) The data file contains the bits in binary format. Each byte of data in the file contains 8 bits of randomly generated data

Tests:

- 01 Frequency Test: Monobit
- 02 Frequency Test: Block
- 03 Cumulative Sums Test
- 04 Runs Test
- 05 Test for the Longest Runs of Ones in a Block
- 06 Binary Matrix Rank Test
- 07 Discrete Fourier Transform (Spectral Test)
- 08 Non-Overlapping Template Matching Test
- 09 Overlapping Template Matching Test
- 10 Maurer's Universal Statistical Test
- 11 Approximate Entropy Test
- 12 Random Excursions Test
- 13 Random Excursions Variant Test
- 14 Serial Test
- 15 Linear Complexity Test

FREQUENCY TEST**COMPUTATIONAL INFORMATION:**

- (a) The nth partial sum = -898
- (b) S_n/n = -0.000898

SUCCESS p_value = 0.369186

BLOCK FREQUENCY TEST**COMPUTATIONAL INFORMATION:**

- (a) χ^2 = 7967.437500
- (b) # of substrings = 7812
- (c) block length = 128
- (d) Note: 64 bits were discarded.

SUCCESS p_value = 0.107356

CUMULATIVE SUMS (FORWARD) TEST

COMPUTATIONAL INFORMATION:

(a) The maximum partial sum = 918

```
SUCCESS          p_value = 0.705472
```

CUMULATIVE SUMS (REVERSE) TEST

COMPUTATIONAL INFORMATION:

(a) The maximum partial sum = 1494

```
SUCCESS          p_value = 0.270336
```

RUNS TEST

COMPUTATIONAL INFORMATION:

(a) $P_i = 0.499551$

(b) $V_{n \text{ obs}}$ (Total # of runs) = 500177

$$(c) \frac{\bar{V}_{n_obs} - 2 n \pi (1-\pi)}{\text{-----}} = 0.250886$$
$$2 \sqrt{2n} \pi (1-p_i)$$

SUCCESS p value = 0.722734

LONGEST RUNS OF ONES TEST

COMPUTATIONAL INFORMATION:

(a) N (# of substrings) = 100

(b) M (Substring Length) = 10000

$$(c) \chi^2 = 3.894568$$

F R E Q U E N C Y

≤ 10	11	12	13	14	15	≥ 16	P-value	Assignment
-----------	----	----	----	----	----	-----------	---------	------------

7 28 22 16 13 6 8

```
SUCCESS          p_value = 0.690942
```

RANK TEST

COMPUTATIONAL INFORMATION:

(a) Probability $P_{32} = 0.288788$

(b) $P_{31} = 0.577576$

(c) $\bar{P}_{30} = 0.133636$

(d) Frequency $F_{32} = 278$

$$(e) \quad F_{31} = 593$$

(f) $\overline{F}_{30} = 105$

(g) # of matrices = 976

(h) $\chi^2 = 6.531766$
 (i) NOTE: 576 BITS WERE DISCARDED.

SUCCESS p_value = 0.038163

FFT TEST

COMPUTATIONAL INFORMATION:

(a) Percentile = 94.965800
 (b) $N_l = 474829.000000$
 (c) $N_o = 475000.000000$
 (d) $d = -1.569204$

SUCCESS p_value = 0.116601

NONPERIODIC TEMPLATES TEST

COMPUTATIONAL INFORMATION

LAMBDA = 244.125000 M = 125000 N = 8 m = 9 n = 1000000

Template Index	F R E Q U E N C Y								χ^2	P_value	Assignment	
	W_1	W_2	W_3	W_4	W_5	W_6	W_7	W_8				
000000001	233	237	232	250	240	239	236	267	4.188479	0.839730	SUCCESS	0
000000011	228	247	235	216	245	241	219	263	9.069123	0.336498	SUCCESS	1
000000101	241	238	271	234	222	221	265	273	13.412770	0.098415	SUCCESS	2
000000111	249	248	255	202	245	235	233	254	9.476903	0.303674	SUCCESS	3
000001001	248	242	253	239	223	243	249	280	7.977121	0.435708	SUCCESS	4
000001011	235	231	270	227	249	237	257	244	6.179714	0.627109	SUCCESS	5
000001101	252	232	227	255	233	255	248	221	5.983768	0.649050	SUCCESS	6
000001111	249	250	235	211	246	229	233	227	7.999364	0.433532	SUCCESS	7
000010001	225	225	262	254	265	250	251	244	7.058823	0.530300	SUCCESS	8
000010011	257	221	238	250	235	279	248	247	8.877414	0.352743	SUCCESS	9
000010101	229	253	229	253	240	256	256	256	4.470217	0.812405	SUCCESS	10
000010111	229	236	264	249	255	256	241	236	4.442679	0.815140	SUCCESS	11
000011001	259	266	253	256	246	243	238	279	9.227998	0.323429	SUCCESS	12
000011011	248	253	214	258	240	233	254	226	7.459188	0.487994	SUCCESS	13
000011101	267	238	218	229	227	233	232	244	8.626391	0.374786	SUCCESS	14
000011111	239	235	225	222	243	208	234	209	15.283260	0.053866	SUCCESS	15
000100011	241	238	245	246	235	236	259	245	1.791582	0.986748	SUCCESS	16
000100101	251	264	258	280	244	221	257	252	11.372813	0.181456	SUCCESS	17
000100111	252	225	231	221	253	272	251	277	13.212587	0.104741	SUCCESS	18
000101001	249	233	279	248	235	228	223	254	9.599766	0.294248	SUCCESS	19
000101011	241	276	236	230	249	237	259	246	6.738954	0.565042	SUCCESS	20
000101101	223	266	274	247	262	239	255	253	10.034025	0.262646	SUCCESS	21
000101111	249	236	237	220	249	253	237	240	3.782817	0.876168	SUCCESS	22
000110011	245	269	247	262	233	246	236	243	4.837748	0.774769	SUCCESS	23
000110101	234	250	250	273	256	266	256	243	7.486727	0.485140	SUCCESS	24
000110111	228	229	226	245	250	243	267	229	6.803564	0.557968	SUCCESS	25
000111001	257	219	262	259	227	238	265	235	9.268247	0.320175	SUCCESS	26
000111011	268	236	231	240	240	250	229	235	5.036872	0.753628	SUCCESS	27
000111101	247	243	275	224	247	247	272	269	11.778474	0.161365	SUCCESS	28

0001111111	239	256	233	241	234	208	237	228	8.554368	0.381270	SUCCESS	29
001000011	266	274	238	218	243	236	253	245	9.481139	0.303345	SUCCESS	30
001000101	219	227	241	251	258	279	232	242	10.769087	0.215129	SUCCESS	31
001000111	238	235	271	245	222	232	251	256	7.069415	0.529162	SUCCESS	32
001001011	265	249	243	280	235	237	249	248	8.137056	0.420198	SUCCESS	33
001001101	224	220	241	245	262	258	220	237	9.076537	0.335881	SUCCESS	34
001001111	243	206	236	254	255	259	258	271	12.170366	0.143763	SUCCESS	35
001010011	249	242	264	253	240	206	228	249	9.559518	0.297312	SUCCESS	36
001010101	243	224	220	243	217	224	231	260	10.823105	0.211925	SUCCESS	37
001010111	243	259	232	225	249	259	239	225	5.814301	0.668024	SUCCESS	38
001011011	233	281	233	239	240	237	249	239	7.419999	0.492068	SUCCESS	39
001011101	230	260	254	226	240	239	258	238	4.875878	0.770756	SUCCESS	40
001011111	248	226	247	240	247	247	257	247	2.369888	0.967522	SUCCESS	41
001100101	268	251	247	229	234	259	230	277	10.415325	0.237076	SUCCESS	42
001100111	238	246	250	251	236	247	219	239	3.620765	0.889618	SUCCESS	43
001101011	237	258	239	264	261	243	246	255	4.543300	0.805086	SUCCESS	44
001101101	252	238	236	256	234	222	249	221	6.173359	0.627820	SUCCESS	45
001101111	234	251	220	233	249	253	241	242	4.119633	0.846172	SUCCESS	46
001110101	234	251	227	226	253	218	240	252	6.828984	0.555192	SUCCESS	47
001110111	255	233	234	241	242	237	223	207	9.465252	0.304579	SUCCESS	48
001111011	268	251	273	207	236	252	242	269	15.169929	0.055924	SUCCESS	49
001111101	240	241	233	252	227	253	235	236	3.109187	0.927320	SUCCESS	50
001111111	263	245	215	245	228	212	235	247	10.971388	0.203326	SUCCESS	51
010000011	248	243	224	258	219	251	248	222	7.612768	0.472180	SUCCESS	52
010000111	244	238	238	215	246	227	244	216	8.520474	0.384346	SUCCESS	53
010001011	231	240	249	236	250	262	252	247	2.979968	0.935608	SUCCESS	54
010001111	214	248	263	259	245	223	259	261	10.393083	0.238513	SUCCESS	55
010010011	250	199	259	242	254	220	222	251	14.882895	0.061463	SUCCESS	56
010010111	249	262	223	266	216	242	239	267	11.070950	0.197711	SUCCESS	57
010011011	233	247	238	261	263	237	235	243	4.007361	0.856459	SUCCESS	58
010011111	227	245	231	264	250	248	251	277	8.638042	0.373744	SUCCESS	59
010100011	253	224	246	245	258	242	267	254	5.532562	0.699430	SUCCESS	60
010100111	235	264	264	258	270	219	238	262	11.539102	0.172983	SUCCESS	61
010101011	235	241	229	251	226	229	245	254	4.340999	0.825122	SUCCESS	62
010101111	227	249	245	241	242	253	251	231	2.670691	0.953296	SUCCESS	63
010110011	250	261	222	245	251	243	244	261	4.841985	0.774324	SUCCESS	64
010110111	216	253	259	221	246	234	271	237	10.612331	0.224647	SUCCESS	65
010111011	252	274	246	231	257	255	250	261	7.344798	0.499929	SUCCESS	66
010111111	226	233	240	255	258	263	255	237	5.530444	0.699665	SUCCESS	67
011000111	252	259	230	237	230	244	256	226	5.095126	0.747362	SUCCESS	68
011001111	250	244	240	243	215	226	210	222	12.216970	0.141783	SUCCESS	69
011010111	257	233	243	232	263	272	279	220	14.274932	0.074875	SUCCESS	70
011011111	247	263	218	259	260	228	271	238	10.761673	0.215572	SUCCESS	71
011101111	271	253	240	242	225	247	247	226	6.496405	0.591806	SUCCESS	72
011111111	245	250	206	243	259	244	242	218	10.161125	0.253899	SUCCESS	73
100000000	233	237	232	250	240	239	236	267	4.188479	0.839730	SUCCESS	74
100010000	258	247	248	242	251	236	256	262	3.364446	0.909452	SUCCESS	75
100100000	237	241	252	250	226	253	251	246	2.606082	0.956600	SUCCESS	76
100101000	243	248	246	224	244	238	265	269	6.426500	0.599571	SUCCESS	77
100110000	218	245	242	230	241	236	253	255	4.915068	0.766614	SUCCESS	78
100111000	236	233	268	254	246	236	250	254	4.486105	0.810822	SUCCESS	79
101000000	232	238	241	213	235	241	230	239	6.278216	0.616099	SUCCESS	80
101000100	272	239	227	267	228	259	231	261	10.837933	0.211052	SUCCESS	81
101001000	249	240	259	239	240	259	252	231	3.223577	0.919553	SUCCESS	82
101001100	240	261	258	222	227	249	233	242	6.054732	0.641101	SUCCESS	83
101010000	257	230	221	246	219	247	247	230	7.417881	0.492289	SUCCESS	84
101010100	277	231	210	239	241	261	202	250	19.265730	0.013501	SUCCESS	85

101011000	210	232	255	264	246	246	211	242	12.428803	0.133073	SUCCESS	86
101011100	272	261	242	219	255	243	238	235	8.210138	0.413217	SUCCESS	87
101100000	254	264	271	257	247	232	248	264	8.244032	0.410003	SUCCESS	88
101100100	239	228	249	250	233	254	246	246	2.427083	0.965044	SUCCESS	89
101101000	250	261	253	250	258	238	237	216	6.373541	0.605466	SUCCESS	90
101101100	241	265	235	207	231	247	242	250	9.009810	0.341469	SUCCESS	91
101110000	235	230	241	249	237	253	249	244	1.989646	0.981328	SUCCESS	92
101110100	215	240	244	217	236	225	248	211	13.324859	0.101150	SUCCESS	93
101111000	235	259	235	234	228	241	243	259	4.163059	0.842120	SUCCESS	94
101111100	262	239	257	238	226	212	284	258	15.642318	0.047795	SUCCESS	95
110000000	239	240	252	232	249	236	231	284	8.915544	0.349471	SUCCESS	96
110000010	229	223	250	226	252	276	257	233	10.191841	0.251819	SUCCESS	97
110000100	221	229	248	275	223	270	259	228	14.103347	0.079111	SUCCESS	98
110001000	241	239	233	239	235	216	262	249	5.946697	0.653203	SUCCESS	99
110001010	261	238	254	237	244	240	240	245	2.141107	0.976377	SUCCESS	100
110010000	258	267	253	245	237	232	256	254	5.217990	0.734043	SUCCESS	101
110010010	259	221	241	243	236	260	244	253	4.930955	0.764930	SUCCESS	102
110010100	240	254	235	239	240	223	254	282	9.402761	0.309466	SUCCESS	103
110011000	231	231	246	229	262	258	246	244	4.628033	0.796491	SUCCESS	104
110011010	256	227	218	252	245	252	230	261	7.311964	0.503378	SUCCESS	105
110100000	237	241	234	233	225	246	241	213	6.925368	0.544706	SUCCESS	106
110100010	250	247	232	263	240	228	221	263	7.262183	0.508627	SUCCESS	107
110100100	264	226	230	239	252	225	264	234	7.942169	0.439140	SUCCESS	108
110101000	263	248	234	239	234	249	252	243	2.921714	0.939174	SUCCESS	109
110101010	269	248	219	247	251	266	215	244	11.216056	0.189755	SUCCESS	110
110101100	202	237	259	267	216	222	221	244	18.578331	0.017285	SUCCESS	111
110110000	244	256	261	249	232	247	253	235	3.248997	0.917774	SUCCESS	112
110110010	234	269	224	241	218	268	243	255	10.626100	0.223798	SUCCESS	113
110110100	259	258	243	261	241	214	214	227	11.938408	0.153973	SUCCESS	114
110111000	218	231	252	236	266	252	235	234	7.241000	0.510868	SUCCESS	115
110111010	214	236	249	220	252	229	236	207	14.041915	0.080679	SUCCESS	116
110111100	233	235	232	223	227	247	253	237	5.216930	0.734159	SUCCESS	117
111000000	259	235	250	219	250	235	235	274	8.743959	0.364354	SUCCESS	118
111000010	218	271	253	274	230	229	280	233	17.858097	0.022316	SUCCESS	119
111000100	248	228	245	220	245	215	265	238	9.236472	0.322742	SUCCESS	120
111000110	243	221	247	225	226	272	245	243	8.548013	0.381846	SUCCESS	121
111001000	250	276	235	218	236	254	242	265	10.253273	0.247698	SUCCESS	122
111001010	249	223	223	218	258	228	247	260	9.793594	0.279813	SUCCESS	123
111001100	215	225	239	225	264	258	249	248	9.457838	0.305156	SUCCESS	124
111010000	261	222	240	220	235	226	261	231	9.499145	0.301952	SUCCESS	125
111010010	229	220	241	222	233	223	253	222	10.372959	0.239818	SUCCESS	126
111010100	232	244	238	253	266	222	287	263	14.514304	0.069307	SUCCESS	127
111010110	214	245	243	248	226	255	228	220	9.377341	0.311470	SUCCESS	128
111011000	260	247	257	245	245	260	248	255	3.443884	0.903501	SUCCESS	129
111011010	258	271	226	244	219	249	213	235	12.499767	0.130259	SUCCESS	130
111011100	234	257	247	240	258	269	249	231	5.511379	0.701779	SUCCESS	131
111100000	261	250	225	209	264	229	256	267	13.586473	0.093201	SUCCESS	132
111100010	246	242	247	223	247	219	258	243	5.490196	0.704126	SUCCESS	133
111100100	251	246	254	219	218	246	221	260	9.542571	0.298609	SUCCESS	134
111100110	253	233	215	253	242	238	248	257	5.729568	0.677495	SUCCESS	135
111101000	246	227	231	264	241	235	236	240	4.406667	0.818697	SUCCESS	136
111101010	240	241	243	249	275	248	265	264	7.841548	0.449099	SUCCESS	137
111101100	245	240	235	261	241	277	242	253	6.607618	0.579497	SUCCESS	138
111101110	245	248	256	230	240	262	254	211	7.997246	0.433739	SUCCESS	139
111110000	270	250	239	280	251	225	270	241	13.174457	0.105986	SUCCESS	140
111110010	255	241	232	217	230	239	239	250	5.496551	0.703422	SUCCESS	141
111110100	240	232	220	250	234	224	255	227	7.200751	0.515136	SUCCESS	142

```

111110110 230 250 230 257 232 254 248 244 3.638771 0.888157 SUCCESS 143
111111000 251 260 229 244 240 211 241 214 10.844288 0.210679 SUCCESS 144
111111010 256 233 220 259 254 238 254 223 7.400934 0.494056 SUCCESS 145
111111100 272 244 228 243 260 227 224 229 9.394288 0.310133 SUCCESS 146
111111110 245 250 206 243 259 244 242 218 10.161125 0.253899 SUCCESS 147
=====

```

OVERLAPPING TEMPLATE OF ALL ONES TEST

COMPUTATIONAL INFORMATION:

```

(a) n (sequence_length)      = 1000000
(b) m (block length of 1s)   = 9
(c) M (length of substring)  = 1032
(d) N (number of substrings) = 968
(e) lambda [(M-m+1)/2^m]     = 2.000000
(f) eta                       = 1.000000
-----

```

```

      F R E Q U E N C Y
    0  1  2  3  4 >=5  Chi^2  P-value  Assignment
-----
359 194 137  97  60 121  4.106682 0.534161 SUCCESS
=====

```

UNIVERSAL STATISTICAL TEST

COMPUTATIONAL INFORMATION:

```

(a) L      = 7
(b) Q      = 1280
(c) K      = 141577
(d) sum     = 877347.519730
(e) sigma   = 0.002768
(f) variance = 3.125000
(g) exp_value = 6.196251
(h) phi     = 6.196964
(i) WARNING: 1 bits were discarded.
-----

```

SUCCESS p_value = 0.796777

=====

APPROXIMATE ENTROPY TEST

COMPUTATIONAL INFORMATION:

```

(a) m (block length)      = 10
(b) n (sequence length)   = 1000000
(c) Chi^2                  = 1083.704253
(d) Phi(m)                 = -6.930968
(e) Phi(m+1)              = -7.623573
(f) ApEn                   = 0.692605
(g) Log(2)                = 0.693147
-----

```

SUCCESS p_value = 0.095242

=====

RANDOM EXCURSIONS TEST

COMPUTATIONAL INFORMATION:

(a) Number Of Cycles (J) = 1730
 (b) Sequence Length (n) = 1000000
 (c) Rejection Constraint = 500.000000

```
=====
SUCCESS      x = -4 chi^2 = 2.121795 p_value = 0.832049
SUCCESS      x = -3 chi^2 = 4.219629 p_value = 0.518247
SUCCESS      x = -2 chi^2 = 7.092899 p_value = 0.213822
SUCCESS      x = -1 chi^2 = 11.611561 p_value = 0.040516
SUCCESS      x = 1 chi^2 = 8.154913 p_value = 0.147902
SUCCESS      x = 2 chi^2 = 0.794205 p_value = 0.977401
SUCCESS      x = 3 chi^2 = 2.269508 p_value = 0.810735
SUCCESS      x = 4 chi^2 = 2.720236 p_value = 0.743022
=====
```

RANDOM EXCURSIONS VARIANT TEST

COMPUTATIONAL INFORMATION:

(a) Number Of Cycles (J) = 1730
 (b) Sequence Length (n) = 1000000

```
=====
SUCCESS      (x = -9) Total visits = 1823; p-value = 0.701378
SUCCESS      (x = -8) Total visits = 1750; p-value = 0.930043
SUCCESS      (x = -7) Total visits = 1755; p-value = 0.906165
SUCCESS      (x = -6) Total visits = 1789; p-value = 0.762328
SUCCESS      (x = -5) Total visits = 1759; p-value = 0.869465
SUCCESS      (x = -4) Total visits = 1688; p-value = 0.787257
SUCCESS      (x = -3) Total visits = 1722; p-value = 0.951500
SUCCESS      (x = -2) Total visits = 1873; p-value = 0.160444
SUCCESS      (x = -1) Total visits = 1833; p-value = 0.079937
SUCCESS      (x = 1) Total visits = 1839; p-value = 0.063874
SUCCESS      (x = 2) Total visits = 1854; p-value = 0.223570
SUCCESS      (x = 3) Total visits = 1760; p-value = 0.819580
SUCCESS      (x = 4) Total visits = 1749; p-value = 0.902831
SUCCESS      (x = 5) Total visits = 1733; p-value = 0.986436
SUCCESS      (x = 6) Total visits = 1737; p-value = 0.971377
SUCCESS      (x = 7) Total visits = 1726; p-value = 0.984952
SUCCESS      (x = 8) Total visits = 1798; p-value = 0.765332
SUCCESS      (x = 9) Total visits = 1967; p-value = 0.328467
=====
```

SERIAL TEST

COMPUTATIONAL INFORMATION:

```
-----
(a) Block length (m) = 16
(b) Sequence length (n) = 1000000
(c) Psi_m = 65563.586560
(d) Psi_m-1 = 32968.732672
(e) Psi_m-2 = 16480.137216
(f) Del_1 = 32594.853888
(g) Del_2 = 16106.258432
-----
```

SUCCESS p_value1 = 0.750144
 SUCCESS p_value2 = 0.938145

 L I N E A R C O M P L E X I T Y

M (substring length) = 500
 N (number of substrings) = 2000

 F R E Q U E N C Y

C0	C1	C2	C3	C4	C5	C6	CHI2	P-value
Note: 0 bits were discarded!								
21	62	281	980	505	114	37	5.788698	0.447272